

Weak lensing by galaxy troughs in DES Science Verification data

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ABSTRACT

We measure the weak lensing shear around galaxy troughs, i.e. the radial alignment of background galaxies relative to underdensities in projections of the foreground galaxy field over a wide range of redshift in Science Verification data from the Dark Energy Survey. Our detection of the shear signal is highly significant (10 to 15σ for the smallest angular scales) for troughs with the redshift range $z \in [0.2, 0.5]$ of the projected galaxy field and angular diameters of $10' \dots 1^\circ$. These measurements probe the connection between the galaxy, matter density, and convergence fields. By assuming galaxies are biased tracers of the matter density with Poissonian noise, we find agreement of our measurements with predictions in a fiducial Λ CDM model. The prediction for the lensing signal on large trough scales is virtually independent of the details of the underlying model for the connection of galaxies and matter. Our comparison of the shear around troughs with that around cylinders with large galaxy counts is consistent with a symmetry between galaxy and matter over- and underdensities. In addition, we measure the two-point angular correlation of troughs with galaxies which, in contrast to the lensing signal, is sensitive to galaxy bias on all scales. The lensing signal of troughs and their clustering with galaxies is therefore a promising probe of the statistical properties of matter underdensities and their connection to the galaxy field.

Key words: gravitational lensing; weak

1 INTRODUCTION

The measurement of weak gravitational lensing probes matter inhomogeneities in the Universe by means of the differential deflection they induce on the light of background sources. Most lensing analyses are driven by the signatures of matter overdensities, e.g. the gravitational shear of galaxies (e.g. Brainerd et al. 1996; Hoekstra et al. 2004; Sheldon et al. 2004; Mandelbaum et al. 2006; van Uitert et al. 2011; Brimiouille et al. 2013; Velander et al. 2014; Clampitt et al. in preparation) and clusters of galaxies (e.g. Tyson et al. 1990; Marrone et al. 2009; Sheldon et al. 2009; Marrone et al. 2012; Hoekstra et al. 2012; von der Linden et al. 2014; Gruen et al. 2014; Umetsu et al. 2014) or the spatial correlation of shear due to intervening large-scale structure, cosmic shear (e.g. Wittman et al. 2000; Fu et al. 2008; Schrabback et al. 2010; Kilbinger et al. 2013; Becker et al. on the arXiv on July 21, 2015).

Probes of underdense structures are complementary to this. Differences between dark energy and modified gravity (MG) models for cosmic acceleration might be more easily differentiable in cosmic voids (Clampitt et al. 2013; Lam et al. 2014; Cai et al. 2014). The reason for this is that the

screening of the hypothetical fifth force of MG (Vainshtein 1972; Khoury & Weltman 2004), required to meet Solar system constraints, is absent in these low density environments. MG therefore entails that negative density perturbations should grow more rapidly than predicted by General Relativity, with effects on the density profile in and around such structures (cf. Cai et al. 2014).

Using voids detected in Sloan Digital Sky Survey (SDSS) spectroscopic galaxy catalogs (Sutter et al. 2012, 2014; Leclercq et al. 2015), first measurements of the radial alignment of background galaxies have been made (Melchior et al. 2014; Clampitt & Jain 2014). Future spectroscopic surveys will yield lensing measurements of void matter profiles with moderate signal-to-noise ratio (Krause et al. 2013). Combined with predictions for void profiles (Hamaus et al. 2014a,b), these will provide unique tests of gravity.

On large enough scales, we expect a symmetry between the excess and deficit of matter relative to the mean. Despite this fact, highly significant lensing measurements have thus far only been performed on matter overdensities. In this work, we follow the new approach of measuring the properties of underdense regions in projections of the galaxy den-

sity field over wide ranges in the radial coordinate, i.e. in redshift. Due to the wide redshift range (e.g. $z \in [0.2, 0.5]$) used for the projection, these can be straightforwardly identified in galaxy catalogues with photometric redshift (photo- z) estimates. Because the selection from the projected field avoids underdensities which are randomly aligned with massive structures in front or behind them along their lines of sight, the signal-to-noise ratio of the lensing signal is comparatively high. The approach is related to and motivated by the measurement of shear around galaxies in underdense projected environments, for which Brimiouille et al. (2013) have previously detected significant radial alignment (cf. their Fig. 25).

We make these measurements using Science Verification (SV) data from the Dark Energy Survey (DES, The Dark Energy Survey Collaboration 2005; Flaugher 2005). The data was taken after the commissioning of the Dark Energy Camera (DECam; DePoy et al. 2008; Flaugher et al. 2015) on the 4m Blanco telescope at the Cerro Tololo Inter-American Observatory (CTIO) in Chile to ensure the data quality necessary for DES. We make use of a contiguous area of 139 sq. deg. for which SV imaging data at lensing quality is available (cf. also Vikram et al. 2015; Jarvis et al. on the arXiv on July 21, 2015).

The structure of this paper is as follows. In Section 2, we describe the data used. Our theoretical modelling of the trough signal is introduced in Section 3. Section 4 presents our measurements of the shear signal around troughs and their angular two-point correlation with galaxies. We summarize and give an outlook to future work in Section 5. For all theory calculations, we use a fiducial flat Λ CDM cosmology ($\Omega_m = 0.3$, $\Omega_b = 0.044$, $\sigma_8 = 0.79$, $n_s = 0.96$).

2 DATA

We select trough positions and measure their lensing signal with galaxy catalogues from the SV phase of DES. In this section, we briefly describe the catalogues used.

2.1 Galaxy catalogue

The DES SVA1 red-sequence Matched Filter Galaxy Catalog (redMaGiC; Rozo et al. on the arXiv on July 21, 2015) is a photometrically selected luminous red galaxy (LRG) sample chosen to have precise and accurate photometric redshifts. redMaGiC makes use of the red sequence model computed from the redMaPPer cluster catalogue (Rykoff et al. 2014; Rykoff et al. in preparation). This model of the red sequence as a function of magnitude and redshift is used to compute the best-fit photo- z for all galaxies regardless of SED type, as well as the χ^2 goodness-of-fit. At any given redshift, all galaxies fainter than a minimum luminosity threshold L_{\min} are rejected. In addition, redMaGiC applies a χ^2 cut such that $\chi^2 < \chi^2_{\max}$, where the maximum $\chi^2_{\max}(z)$ is chosen to ensure that the resulting galaxy sample has a nearly constant comoving space density \bar{n} . In this work, we use the *high density* sample, such that $\bar{n} = 10^{-3} h^3 \text{Mpc}^{-3}$ and $L_{\min}(z) = 0.5 L_*(z)$ in the assumed cosmology. This space density is roughly 4 times that of the SDSS BOSS CMASS sample. As detailed in Rozo et al. (on the arXiv on July 21, 2015), the redMaGiC photo- z s are nearly unbiased,

with a scatter of $\sigma_z/(1+z) \approx 1.7\%$ and a 4- σ outlier rate of about 1.7%. By virtue of this, redshift errors are negligible for the selection of underdensities in the galaxy field when the latter is projected over the wide redshift ranges we use (see Section 2.2).

2.2 Trough selection

The troughs are selected as centres of cylindrical regions (or, more accurately, of conical frustums) of low galaxy density as follows. Let the galaxy catalogue (cf. Section 2.1) be given with entries \mathbf{x}_i, z_i, L_i for the angular position, redshift and luminosity of galaxy i , $1 \leq i \leq n$.

Define a function $W_z(z, L)$ that assigns a weight to each galaxy based on its redshift and luminosity. Furthermore, define $W_T(\theta)$ to weight points by their projected angular separation θ from the centre. From these we define a projected, weighted and smoothed version of the galaxy density field

$$G(\mathbf{x}) = \sum_{i=1}^n W_T(|\mathbf{x} - \mathbf{x}_i|) W_z(z_i, L_i). \quad (1)$$

In this study, we use a simple weighting corresponding to a hard cut in luminosity, redshift and radius, i.e.

$$W_z(z, L) = \begin{cases} 1, & L \geq 0.5 L^* \wedge 0.2 \leq z \leq 0.5 \\ 0, & \text{otherwise} \end{cases} \\ W_T(\theta) = \begin{cases} 1, & \theta \leq \theta_T \\ 0, & \text{otherwise} \end{cases} \quad (2)$$

with some trough radius θ_T , which we vary between 5 and 30 arcmin. The redshift range of $z \in [0.2, 0.5]$ is motivated by a trade-off between having a large trough volume (and hence a large signal) and having sufficient background galaxies with useful shear estimates to measure the effect, although we test other settings in Section 4.1.1. Note that a luminosity-independent weighting scheme of LRGs, as we apply it here, is not far from optimal for the reconstruction of the matter field (Cai et al. 2011).

Probed on a finely spaced grid of sky positions, for which we use an $N_{\text{side}} = 4096$ HEALPIX (Górski et al. 2005) map with 0.86 arcmin pixel spacing, there is a distribution of weighted galaxy counts as measured by G . We select the set of trough positions T as the points below the 20th percentile G_{20} of that distribution, i.e. $T = \{\mathbf{x} : G(\mathbf{x}) \leq G_{20}\}$.¹ It is important to note that we are *not* selecting individual minima of the galaxy density field. Instead, troughs are overlapping within and between samples of fixed trough radius. A map of trough positions for $\theta_T = 10'$ is shown in Figure 1. Note how the troughs visibly trace underdensities in the convergence field.

In practice, G needs to be corrected for the effect of masking due to survey boundaries or bright stars, for example. A homogeneous masking fraction over all cylinders simply decreases the tracer density, which is accounted for by our model automatically. When masking fractions are not

¹ We have also tried stricter (i.e. lower percentile) and looser (i.e. higher percentile) thresholds, which yield a higher (lower) amplitude of the signal with larger (smaller) uncertainties. Also see Section 4.1.2 for the selection of *high* density cylinders.

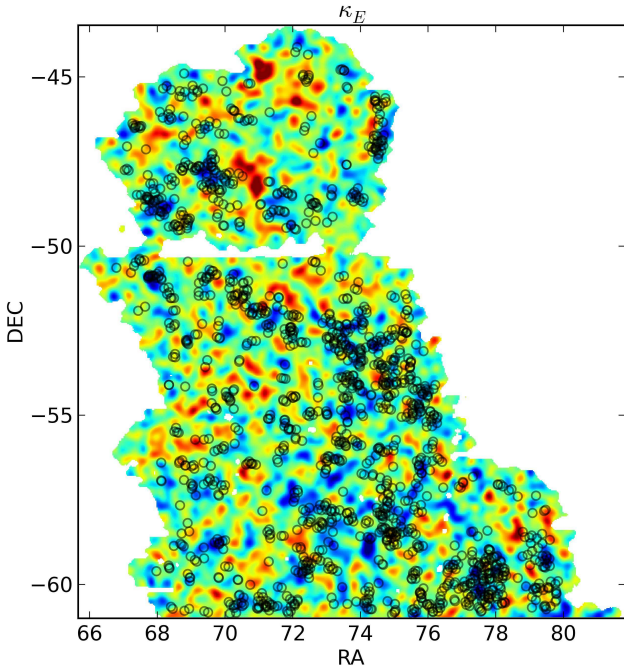


Figure 1. Positions of 10' troughs (black circles, to scale, randomly selected sample of 1500 out of the $\approx 110,000$ trough positions probed) overlaid onto lensing convergence map (red: positive, blue: negative). Convergence was estimated as described in Vikram et al. (2015) with a weighted lensing source catalogue (Section 2.3) and a 7' Gaussian smoothing.

homogeneous but vary among the cylinders, the situation is more complicated. For the present analysis, we make the approximation of excluding all cylinders where more than $f = 20\%$ of the area inside the trough radius is masked in the galaxy catalogue and assume that all remaining cylinders have equal masking fractions when selecting troughs and modelling the signal. At the level of statistical precision achieved here, this simplification is not expected to cause a significant difference.

The mean surface density of redMaGiC galaxies in the useable area is approximately $\bar{n} = 0.055 \text{ arcmin}^{-2}$, corresponding to a mean count of approximately 4, 17, 69 and 155 galaxies in cylinders of radius 5', 10', 20' and 30'. At the lower 20th percentile, selected troughs have mean counts of 1, 9, 44 and 108 galaxies, respectively.

2.3 Lensing source catalogue

For the background sources, we use a shape catalogue measured with NGMIX.² We apply the cuts, weighting and responsivity correction as recommended in Jarvis et al. (on the arXiv on July 21, 2015), where also the shape measurement and testing of catalogues is described in detail. In order to prevent confirmation bias, shear estimates in the catalogue were blinded with an unknown factor until the analysis had been finalized (cf. Jarvis et al. on the arXiv on July 21, 2015, their Section 7.5).

We use the two highest redshift bins defined in Becker et

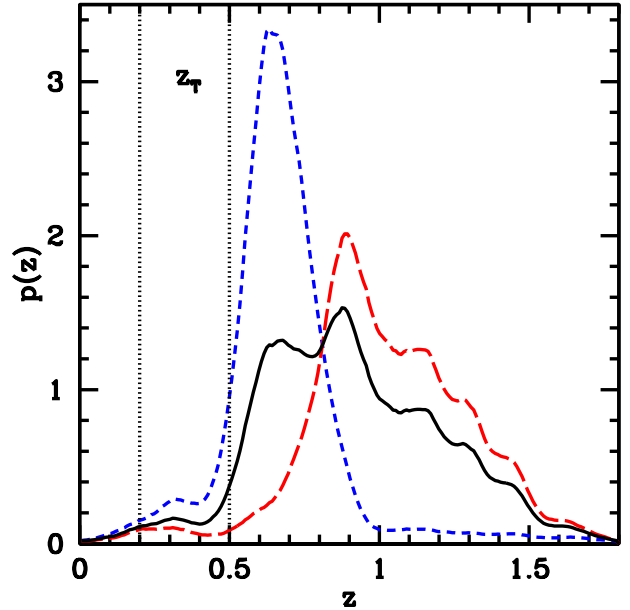


Figure 2. Redshift distributions of the low redshift lensing source sample (blue, short dashed line), high redshift sample (red, long dashed line) and the combined fiducial source sample (black, solid line). All distributions are weighted by inverse shape noise of the sources in analogy to the shear signal and normalized for $\int p(z) dz = 1$. The fiducial trough redshift range is indicated by the dotted vertical lines.

al. (on the arXiv on July 21, 2015, cf. their Fig. 3) by means of photo- z probability density estimates made with SKYNET (Graff & Feroz 2013; Bonnett 2015), a method that performed well in an extensive set of tests on SV data (Sánchez et al. 2014). The mean redshift of the lower (higher) redshift bin is $z \approx 0.6$ ($z \approx 0.9$). We use the appropriately weighted SKYNET stacked $p(z)$ estimate for predicting the lensing signal (cf. Section 3). To maximize the signal-to-noise ratio for our non-tomographic measurements, we weight the signal measured in both bins as 1:2 to approximately accommodate the ratio of effective inverse critical surface mass density. The resulting $p(z)$ of the samples used are shown in Figure 2. The tests performed in Bonnett et al. (on the arXiv on July 21, 2015) indicate that errors in photo- z estimation are not a dominant systematic error for the prediction of the shear power spectrum that we use them for.

We note that the consistency of different shape measurement and photo- z methods with the catalogues used in this analysis has been investigated in detail and confirmed within the systematic requirements on the present data in several works (Sánchez et al. 2014; Jarvis et al. on the arXiv on July 21, 2015; Bonnett et al. on the arXiv on July 21, 2015; Becker et al. on the arXiv on July 21, 2015; The Dark Energy Survey Collaboration et al. on the arXiv on July 21, 2015).

3 THEORY

Structures in the Universe can be described by an underlying field, the matter density as a function of position and

² cf. <https://github.com/esheldon/ngmix>

time. Matter density itself is not an observable. Its properties can, however, be recovered by a number of observable fields, such as the three-dimensional or projected galaxy density (a sparse, biased tracer) or the convergence field (a weighted, projected version of it). In this section we describe our modelling of the shear and galaxy correlation signal of troughs by the interrelation of these observables and the underlying matter density.

We assume that the three-dimensional galaxy field can be described as a deterministic, biased tracer of the matter. This means that the the 3D contrast δ of matter density ρ ,

$$\delta = \frac{\rho - \langle \rho \rangle}{\langle \rho \rangle}, \quad (3)$$

and the equivalent quantity defined for the galaxy field are proportional at any position. Their ratio defines the bias b , which depends on the galaxy population.

Lensing convergence κ is related to δ via the projection integral over comoving distance χ (cf., e.g. Bartelmann & Schneider 2001):

$$\kappa(\boldsymbol{\theta}) = \int_0^\infty d\chi q_\kappa(\chi) \delta(\chi\boldsymbol{\theta}, \chi), \quad (4)$$

where

$$q_\kappa(\chi) = \frac{3H_0^2\Omega_m^0}{2} \chi \mathcal{G}(\chi) \quad (5)$$

with

$$\mathcal{G}(\chi) = \int_\chi^\infty d\chi' n_{\text{source}}(\chi') \frac{\chi' - \chi}{\chi'}. \quad (6)$$

Here $n_{\text{source}}(\chi)$ is the distribution of source galaxies of the lensing measurement.

An overdensity of convergence inside a circular aperture relative to its edge results in a tangential alignment of background galaxy shapes. Correspondingly, an underdensity causes radial alignment. Both cases are described by (cf. Schneider et al. 2006, p. 279f)

$$\gamma_t(\theta) = \langle \kappa \rangle(< \theta) - \kappa(\theta). \quad (7)$$

Here, $\gamma_t(\theta)$ is the tangential component of gravitational shear averaged over the edge of a circle of radius θ , $\kappa(\theta)$ is the equivalent average of the convergence and $\langle \kappa \rangle(< \theta)$ is the mean convergence inside the circle. For the case of $|\gamma_t| \ll 1$, $|\kappa| \ll 1$, tangential components of gravitational shear and reduced shear g_t are approximately equal and observable as the mean tangential alignment of background galaxy ellipticity. The cross component of shear, γ_\times , rotated by 45° relative to the tangential direction, is expected to be zero when taking the average over the full circle for a single thin lens or over an ensemble of thick lenses.

In order to connect these fields and model the trough signal, we make these three assumptions:

- We apply the Limber (1954) approximation to compute the angular power spectrum of the *projected matter density contrast* $\delta_\Sigma(\boldsymbol{\theta})$ within the redshift range of the redMaGiC galaxies used for the trough selection ($0.2 \leq z \leq 0.5$). The same approximation is also used to compute the cross power spectrum between δ_Σ and the convergence field $\kappa(\boldsymbol{\theta})$ relative to the background galaxy redshift distribution.

- We assume that $\delta_\Sigma(\boldsymbol{\theta})$ and $\kappa(\boldsymbol{\theta})$ follow a Gaussian distribution - at least when they are averaged over the trough radius or over the annuli in which we measure the shear.

- We assume that the redMaGiC galaxies are placed onto δ_Σ via a biased Poisson process.

In this section we describe how these assumptions translate to a prediction for the expected shear signal and galaxy density around troughs.

3.1 Projected matter density and galaxy counts

Let the volume density of redMaGiC galaxies as a function of comoving distance χ be given by $n_{\text{lens}}(\chi)$. The projected galaxy contrast is proportional to a weighted projection of matter contrast δ_Σ . In a flat universe, the latter is calculated as

$$\delta_\Sigma(\boldsymbol{\theta}) = \frac{\Sigma - \bar{\Sigma}}{\bar{\Sigma}} = \int_{\chi_0}^{\chi_1} d\chi n_{\text{lens}}(\chi) \delta(\chi\boldsymbol{\theta}, \chi), \quad (8)$$

where $\delta(\chi\boldsymbol{\theta}, \chi)$ is the 3D matter contrast at the point $(\chi\boldsymbol{\theta}, \chi)$ on the backward light cone. For a galaxy sample with constant comoving density, such as the redMaGiC catalogue, this is a simple volume weighting of matter density, $n_{\text{lens}}(\chi) \propto dV/[d\Omega d\chi]$, and δ_Σ is the common projected matter density contrast.

If we average δ_Σ over circles of angular radius θ_T , we arrive at the new random field δ_T ,

$$\delta_T(\boldsymbol{\theta}) = \frac{1}{\pi\theta_T^2} \int_{|\boldsymbol{\theta}-\boldsymbol{\theta}'| \leq \theta_T} d^2\boldsymbol{\theta}' \delta_\Sigma(\boldsymbol{\theta}'). \quad (9)$$

In this we have made the approximation of a flat sky, valid for $\theta_T \ll 1$.

If the galaxies are placed onto $\delta_\Sigma(\boldsymbol{\theta})$ via a biased Poisson process, then the discrete probability P of finding N galaxies within θ_T given the value of δ_T is

$$P(N|\delta_T) = \frac{1}{N!} (\bar{N} [1 + b\delta_T])^N \exp(-\bar{N} [1 + b\delta_T]), \quad (10)$$

For $\delta_T < -\frac{1}{b}$ we assume $P(N > 0|\delta_T) = 0$ and $P(N = 0|\delta_T) = 1$ (see also Appendix A). We have used the bias b and mean galaxy count \bar{N} within θ_T . For our model predictions shown later, we fix the bias at a fiducial value of $b = 1.6$ or vary it between 1.4...1.8 to show the dependence on bias in the relevant range. Note that we neglect the moderate redshift dependence of the bias of redMaGiC galaxies (cf. Rozo et al. on the arXiv on July 21, 2015), which is a good approximation for the limited redshift range used here.

We identify troughs as circles in the sky with low galaxy count N . Given any N , the expected value of δ_T is

$$\langle \delta_T | N \rangle = \int_{-1}^\infty d\delta_T \delta_T p(\delta_T | N). \quad (11)$$

Bayes' theorem tells us that

$$p(\delta_T | N) = \frac{P(N|\delta_T)p(\delta_T)}{P(N)}. \quad (12)$$

When the variance $\text{Var}(\delta_T) := \sigma_T^2 \ll 1$, we can approximate $p(\delta_T)$ by a Gaussian distribution, i.e.

$$p(\delta_T) = \frac{1}{\sqrt{2\pi\sigma_T^2}} \exp\left(-\frac{\delta_T^2}{2\sigma_T^2}\right). \quad (13)$$

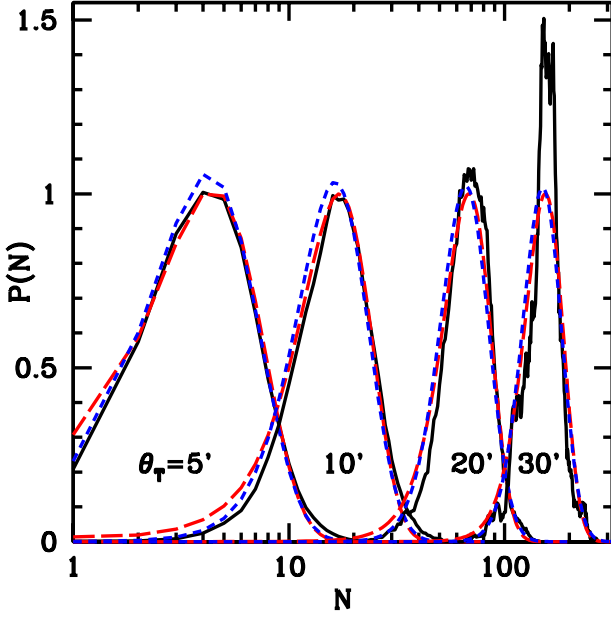


Figure 3. Distribution of redMaGiC galaxy counts in $z_T \in [0.2, 0.5]$ for various trough radii θ_T . We show measurements (black, solid line) and model predictions for Gaussian matter fields onto which galaxies are placed as biased tracers with $b = 1.6$ and Poissonian noise (red, long-dashed lines). Model predictions for a log-normal matter density are also shown (blue, short-dashed lines). Normalization of $P(N)$ is matched to make $\max(P^{\text{Gaussian}}) = 1$ for each trough radius.

In Appendix B we derive how σ_T^2 can be calculated from the power spectrum of δ_Σ , which in the Limber (1954) approximation is related to the 3D matter power spectrum P_δ by (cf., e.g. Bartelmann & Schneider 2001, Eqn. 2.84)

$$C_\Sigma(\ell) = \int_0^\infty d\chi \frac{m_{\text{lens}}(\chi)^2}{\chi^2} P_\delta\left(\frac{\ell}{\chi}, \chi\right). \quad (14)$$

For our calculations we use the non-linear matter power spectrum P_δ from Smith et al. (2003).

The normalisation factor in equation 12, $P(N)$, gives the probability of finding N galaxies inside a cylinder of radius θ_T . Figure 3 shows the observed distribution of galaxy counts in cylinders. There is reasonable agreement to our prediction from a Gaussian random field δ_T onto which galaxies are placed by means of equation 10 (dashed, red lines). The distribution of counts inside 30 arcmin radii appears more peaked than the model, potentially explained by the fact that there is too little area to have enough uncorrelated troughs at this scale.

As an alternative prescription, we also calculate the expected $P(N)$ for the case of a log-normally distributed matter density. This is done by replacing the Gaussian $p(\delta_T)$ of equation 13 by a shifted log-normal distribution of the same variance with a minimum value of $\delta_T = -1$. The result (dotted, blue lines in Figure 3) resembles the low density tail of the galaxy count distribution more closely.

3.2 Convergence and shear profile

Our goal is to compute the mean value of κ at a distance θ from the trough centre. For this we define a set of annuli $i = 1 \dots n$ around the trough for which $\theta \in [\theta_i, \theta_{i+1})$. Let K_i be the average of κ in annulus A_i ,

$$K_i(\theta) = \frac{1}{\pi(\theta_{i+1}^2 - \theta_i^2)} \int_{A_i} d^2\theta' \kappa(\theta'). \quad (15)$$

If both δ_T and K_i have Gaussian distributions with zero mean, then the expectation value of K_i for a fixed value of δ_T is given by

$$\langle K_i | \delta_T = s \rangle = \frac{\text{Cov}(\delta_T, K_i)}{\sigma_T^2} s, \quad (16)$$

where the covariance $\text{Cov}(\delta_T, K_i)$ can be computed in terms of the cross power spectrum $C_{\kappa, \Sigma}(\ell)$ of Σ and κ (see Appendix B). Note that the Gaussian approximation for the matter contrast and convergence becomes accurate regardless of the pointwise $p(\delta)$ since all random fields are smoothed over annuli or circles and a large redshift range.

The expectation value of K_i when the trough contains N galaxies is finally given by

$$\begin{aligned} \langle K_i | N \rangle &= \int_{-1}^\infty ds \langle K_i | \delta_T = s \rangle p(\delta_T = s | N) \\ &= \frac{\text{Cov}(\delta_T, K_i)}{\sigma_T^2} \int_{-1}^\infty ds s p(\delta_T = s | N) \\ &= \frac{\text{Cov}(\delta_T, K_i)}{\sigma_T^2} \langle \delta_T | N \rangle. \end{aligned} \quad (17)$$

If we select as troughs all cylinders with $N \leq N_{\text{max}}$ galaxies, the mean K_i around them will be

$$\langle K_i | \leq N_{\text{max}} \rangle = \frac{\text{Cov}(\delta_T, K_i)}{\sigma_T^2} \frac{\sum_{N=0}^{N_{\text{max}}} P(N) \langle \delta_T | N \rangle}{\sum_{N=0}^{N_{\text{max}}} P(N)}. \quad (18)$$

The tangential shear signal around troughs is given by equation 7, using equation 18 to calculate the mean convergence in each annulus.

3.3 Trough-galaxy angular correlation

The trough-galaxy angular correlation function can be modelled in a very similar way. First define annuli A_i around the trough that correspond to the bins in which $w(\theta)$ is measured. The mean density contrast w_i in each annulus is given by (cf. equation 15)

$$w_i(\theta) = \frac{1}{\pi(\theta_{i+1}^2 - \theta_i^2)} \int_{A_i} d^2\theta' \delta_\Sigma(\theta'). \quad (19)$$

Under the assumptions of Gaussianity the expectation value of δ_i for a fixed value of δ_T is given by (cf. equation 16)

$$\langle w_i | \delta_T = s \rangle = \frac{\text{Cov}(\delta_T, w_i)}{\sigma_T^2} s. \quad (20)$$

In analogy to equation 18, the mean density contrast in annulus A_i around the trough is given by

$$\langle w_i | \leq N_{\text{max}} \rangle = \frac{\text{Cov}(\delta_T, w_i)}{\sigma_T^2} \frac{\sum_{N=0}^{N_{\text{max}}} P(N) \langle \delta_T | N \rangle}{\sum_{N=0}^{N_{\text{max}}} P(N)}. \quad (21)$$

The average number of galaxies in an annulus i *outside* the trough radius is given by

$$\begin{aligned} \langle N_i | \leq N_{\max} \rangle_{\text{out}} &= \bar{N} \frac{A_i}{A_T} [1 + b(w_i | \leq N_{\max})] \\ &= \bar{N}_i [1 + b(w_i | \leq N_{\max})], \end{aligned} \quad (22)$$

where the mean galaxy count \bar{N}_i in annulus i is obtained by rescaling the average galaxy count inside one trough radius to the area A_i of the annulus,

$$\bar{N}_i = \bar{N} \frac{A_i}{A_T}. \quad (23)$$

The profile of galaxy counts around a trough is then given by

$$\begin{aligned} \langle w_{N,i} | \leq N_{\max} \rangle_{\text{out}} &= \frac{\langle N_i | \leq N_{\max} \rangle_{\text{out}}}{\bar{N}_i} - 1 \\ &= b(w_i | \leq N_{\max}). \end{aligned} \quad (24)$$

The situation is more complicated for annuli *inside* the trough radius θ_T . Here the Poisson noise of the different bins is correlated. This is because the sum of the galaxy counts in the different bins has to meet the requirement by which we selected the troughs.

Without full treatment of the covariances, we make a prediction for the galaxy number counts inside the trough that (i) matches the mean galaxy counts predicted by the full model and (ii) matches the projected matter contrast profile with a given bias. To this end, we simply replace \bar{N} in equation 22 by the predicted mean number of galaxies inside *selected* troughs, e.g. when demanding that $N_T \leq N_{\max}$. This number is given by

$$\bar{N}_T = \frac{\sum_{N=0}^{N_{\max}} P(N) N}{\sum_{N=0}^{N_{\max}} P(N)}. \quad (25)$$

The mean number of galaxies found in an annulus inside the trough is then given by

$$\langle N_i | \leq N_{\max} \rangle_{\text{in}} = \bar{N}_T \frac{A_i}{A_T} [1 + b(w_i | \leq N_{\max})] \quad (26)$$

and the profile of galaxy counts inside the trough radius is given by

$$\begin{aligned} \langle w_{N,i} | \leq N_{\max} \rangle_{\text{in}} &= \frac{\langle N_i | \leq N_{\max} \rangle_{\text{in}}}{\bar{N}_i} - 1 \\ &= \frac{\bar{N}_T}{\bar{N}} [1 + b(w_i | \leq N_{\max})] - 1. \end{aligned} \quad (27)$$

4 MEASUREMENT

In the following section, we correlate trough positions with the shear signal of background galaxies (Section 4.1). Additionally, we measure the projected number density profile of redMaGiC galaxies in the same redshift and luminosity range used for the trough selection, i.e. the angular two-point cross-correlation of troughs and galaxies (Section 4.2).

4.1 Shear signal

We measure the mean shear of background galaxies around troughs, selected as described in Section 2.2. To correct for potential additive shear systematic errors, we subtract the

tangential shear measured around random points that pass our masking selection criterium for the respective trough radius from the trough shear signal. Fig. 4 shows measured tangential and cross shears.

Per-mille radial alignment of background galaxies at and beyond the trough radius is detected with high significance in all bins (cf. Section 4.1.3). Cross shears are consistent to the expected null signal within the uncertainties (cf. also the reduced χ^2_{\times} in Table 1). The model proposed in Section 3 is a good fit to the data in all bins (cf. Section 4.3 and reduced χ^2_{mod} in Table 1).

4.1.1 Tomography

By splitting either the source sample or using smaller redshift ranges for selecting the troughs, it is possible to probe the redshift evolution of the trough lensing signal. We perform both measurements in the following.

- For source tomography, we divide the source galaxy sample into two redshift bins (cf. Section 2.3). Note that since troughs are thick lenses, the change in source redshift causes more than a simple change in amplitude. The differential weighting as a function of lens redshift inside the $z = 0.2 \dots 0.5$ cylinder also influences the shape of the shear profile. Due to the nearly power-law matter two-point correlation of the matter at all redshifts, however, the latter effect is small. The left panel of Fig. 5 shows the source-tomographic signal. We note that the agreement of the measurement with the model in both bins is additional evidence for the appropriateness of the $p(z)$ s as estimated for our source samples (cf. Bonnett et al. on the arXiv on July 21, 2015).

- For trough redshift tomography, we split the trough redshift range into two approximately equal-volume slices $z = 0.2 \dots 0.4$ and $z = 0.4 \dots 0.5$. When using these smaller redshift ranges for the trough selection, two effects reduce the signal-to-noise ratio: (1) due to the lower galaxy count, Poissonian noise weakens the correlation of trough positions with matter underdensity; and (2) uncorrelated, overdense large-scale structure along the line of sight outside the trough redshift range causes additional variance in the lensing signal. Shear measurements are shown in the right panel of Fig. 5. The signal is reduced as expected, but the measurement is still highly significant and consistent with the model in both cases.

4.1.2 Galaxy density percentiles

All measurements presented above use troughs selected to be below the lower 20th percentile of galaxy counts. Measurements with larger limiting percentiles (e.g. the 30th percentile) give results of similar significance but smaller amplitude.

It is particularly interesting, however, to study the symmetry of matter in the overdense and underdense tails of the galaxy field. For dense enough tracers and large enough scales, the expectation is that all involved fields are approximated well by a Gaussian distribution. This should lead to symmetric shear signals at the same upper and lower percentiles. On smaller scales, the galaxy counts (if only due to Poisson noise) and the matter density and convergence field

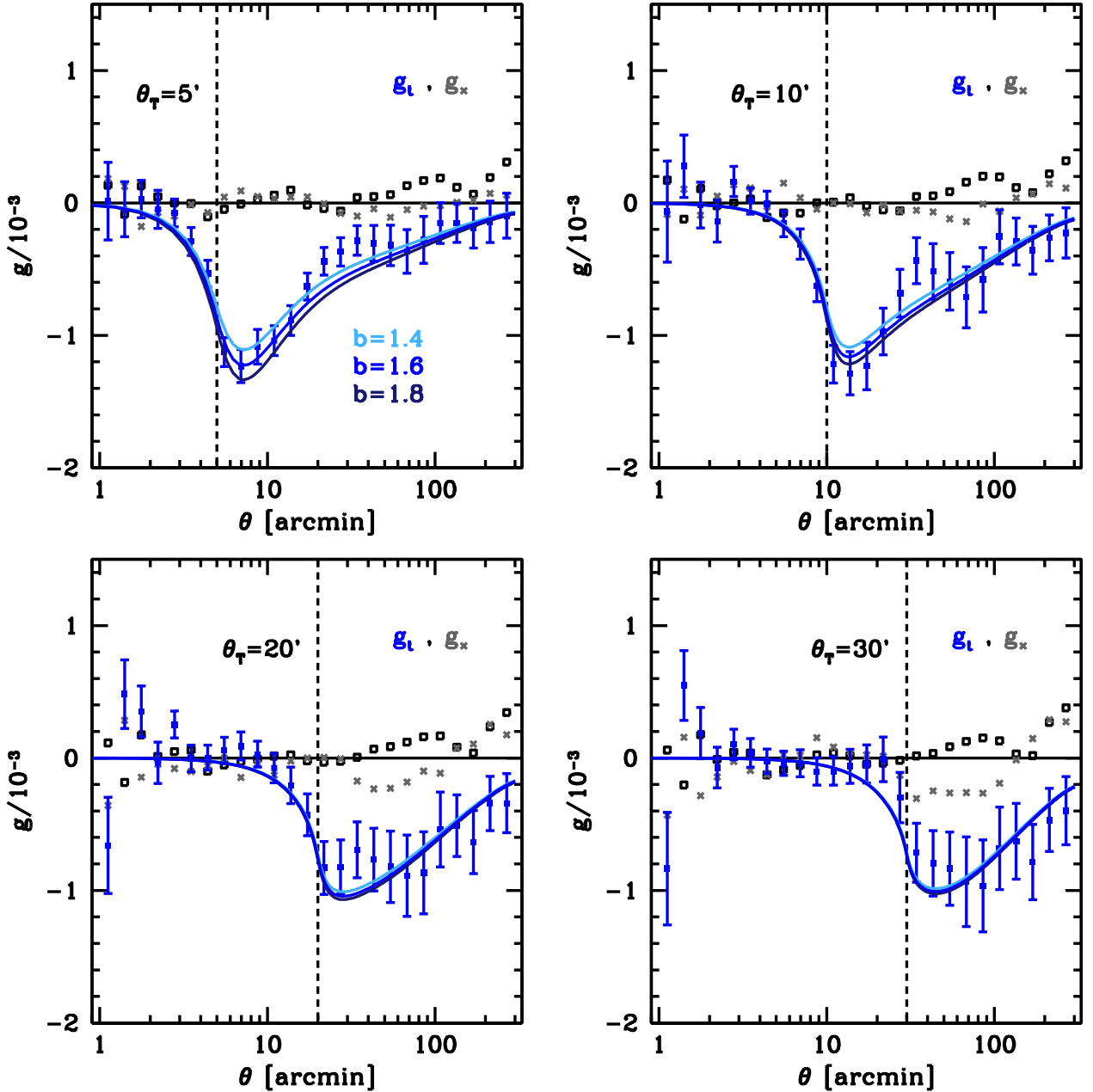


Figure 4. Weak lensing signal of galaxy troughs of $\theta_T = 5, 10, 20$ and 30 arcmin radius (top left to bottom right). Shown is the tangential shear signal (blue) around points from the lower 20th percentile in galaxy counts in cylinders of $z = 0.2 \dots 0.5$. Lines show model predictions (cf. Section 3) for our fiducial cosmology and, for illustration of the bias dependence, a bias of $b = 1.4, 1.6, 1.8$ (light to dark blue). Cross-shear is shown with grey cross symbols, to be interpreted with error bars of similar size. Tangential shear around random points, subtracted from the trough measurement, is shown with black open symbols.

(since $|\delta| \ll 1$ is no longer true and non-linear evolution boosts high density fluctuations) deviate from a Gaussian distribution and we expect some degree of asymmetry between the low and high density signal.

The measurement for both the lower and upper 20th percentile is shown in Fig. 6 and is in agreement with these expectations. At small trough radii, there appears to be a significant asymmetry, with the overdense regions showing a larger shear signal than anticipated from our model or the measurement of underdensities. For larger cylinders, such

an effect is not detected. A log-normal model of the matter contrast (dashed lines) leads to a slightly improved prediction of the shear signal on small scales, although there is still a discrepancy near 10 arcmin. The difference between the models on large scales is negligible.

4.1.3 Significance

For estimating uncertainties, we use a set of $N_j = 100$ jack-knife resamplings. In order to ensure that these are approxi-

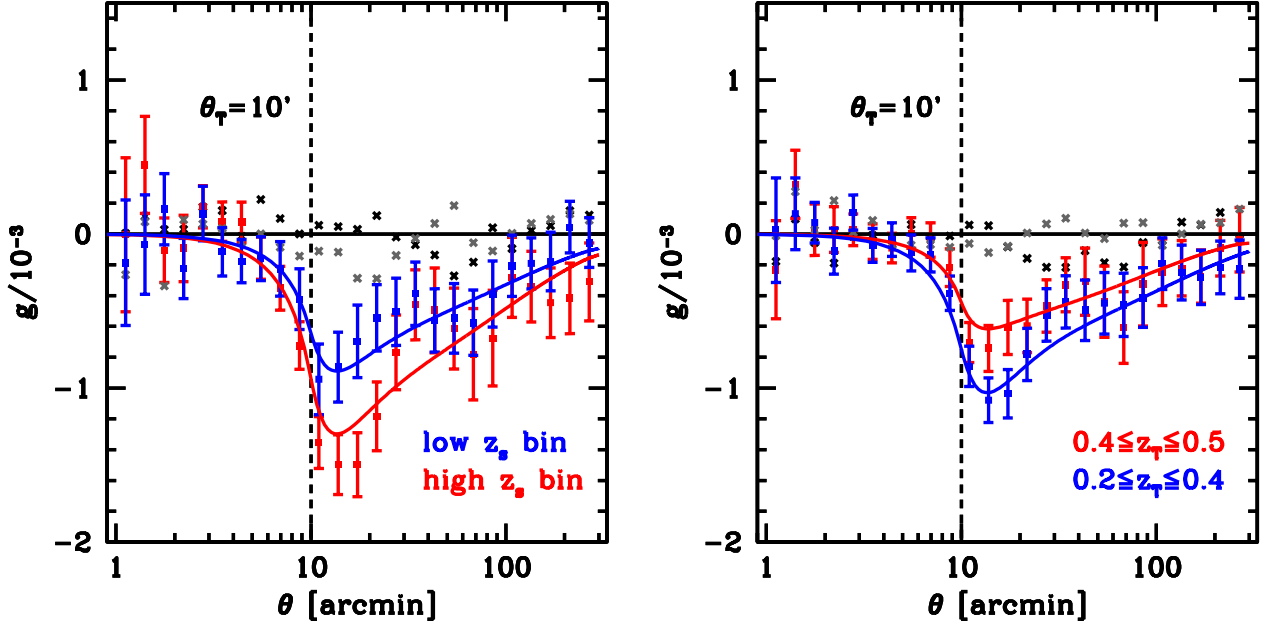


Figure 5. Source tomography (left) and trough redshift range tomography (right) of trough lensing signal. Left panel shows signal for sources in our two redshift bins (cf. Section 2.3). Right panel shows signal of troughs selected by the galaxy count in $z_T = 0.2 \dots 0.4$ (blue) and $z = 0.4 \dots 0.5$ (red). Lines show model predictions of the respective tangential shear signal (cf. Section 3) for a bias of $b = 1.6$ and grey/black points indicate g_x for both measurements.

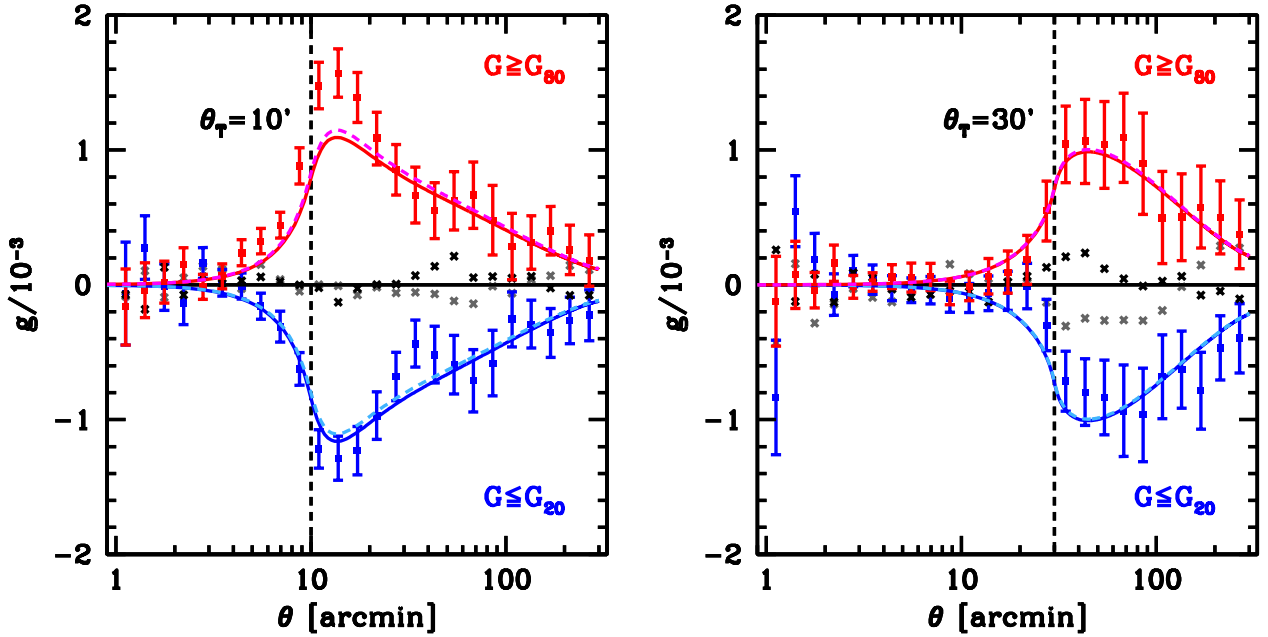


Figure 6. Tangential shear signal for troughs, i.e. centres of cylinders below the 20th (measurement and model in blue), and overdense cylinders above the 80th percentile (red) in galaxy count. We plot model predictions for a bias of $b = 1.6$, with solid lines assuming a Gaussian and dashed lines a log-normal distribution of the matter contrast. Grey/black points indicate g_x for both measurements

mately equally populated with troughs, we choose them with a K-means algorithm³ on the catalogue of 5 arcmin trough

positions. The delete-one jackknife yields a covariance

$$\text{Cov}(f_1, f_2) = \frac{N_j - 1}{N_j} \sum_{i=1}^{N_j} (f_{1,-i} - \langle f_1 \rangle)(f_{2,-i} - \langle f_2 \rangle) \quad (28)$$

for two quantities f_1, f_2 estimated from the data excluding region i (f_{-i}) or averaging over all ($\langle f \rangle = N^{-1} \sum_{i=1}^N f_{-i}$). In

³ https://github.com/esheldon/kmeans_radec/

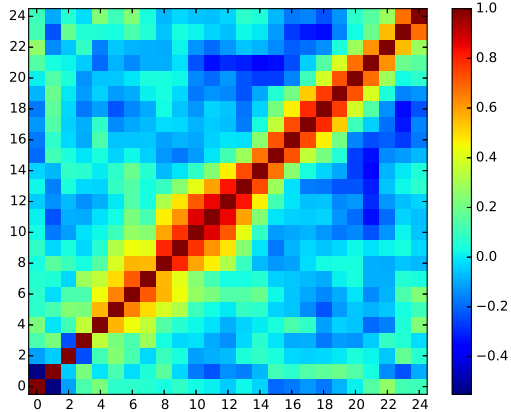


Figure 7. Correlation matrix R_{ij} of shear around 10 arcmin troughs measured in the logarithmic angular bins of Fig. 4 as estimated from 100 jackknife regions.

our case, we estimate the covariance matrix $\hat{\mathbf{C}}$ of tangential shear measurements (or, in Section 4.2, angular two-point correlation measurements) in our set of angular bins.

Figure 7 shows the correlation coefficients $R_{ij} = \text{Cov}(g_t^i, g_t^j) / \sqrt{\text{Var}(g_t^i)\text{Var}(g_t^j)}$ estimated for our fiducial 10 arcmin trough measurement. At intermediate and large radii, neighboring bins are highly positively correlated, which is even more the case for the larger troughs. The negative correlation of the innermost bins is a generic feature that appears in all trough sizes probed and is connected to the opposite sign of the first two data points of the lower panels of Fig. 4.

We ensure the significances defined below are stable under a change of binning scheme and jackknife regions by calculating them with 15 instead of 25 radial bins for which we estimate the covariance using 50 rather than 100 jackknife patches, which yields consistent results.

Different measures of detection significance can be defined as follows:

(i) **Signal-to-noise (SNR) of shear.** A simple measure is the tangential shear at the first angular bin outside the trough radius θ_T in units of its standard deviation according to the jackknife estimate, $g_t/\sigma_g := |g_t(\theta_T)|/\sigma_{g_t(\theta_T)}$.

(ii) For **optimal signal-to-noise** (cf., e.g. Gruen et al. 2011, their Eqn. 11), we define a linear combination of tangential shear measurements. The weights of the linear combination are chosen as $\mathbf{W} \propto \hat{\mathbf{C}}^{-1} \mathbf{g}_t^{\text{model}}$, where we use the model prediction $\mathbf{g}_t^{\text{model}}$ for our fiducial bias of $b = 1.6$. The SNR of $\Gamma = \mathbf{W} \cdot \mathbf{g}_t$ is given as $\Gamma/\sigma_\Gamma = \Gamma/\sqrt{\mathbf{W}^T \cdot \hat{\mathbf{C}} \cdot \mathbf{W}}$.

(iii) We do not list a significance based on the χ^2 of the null hypothesis here for two reasons: (I) since the signal is consistent with zero on a range of small and large scales, as is also expected from the model, the p -values of the measured χ^2 strongly depend on which bins are used and (II) χ^2 yields an uncertain estimate of SNR due to the variance $\text{Var}(\chi^2) = 2n_{\text{bins}}$ for n_{bins} bins.

We list these metrics for various trough selections in Table 1. For the most conservative metric, g_t/σ_g , we find a detection significance of 10σ for the smallest troughs. The optimal

θ_T	Trough selection $z_T \in \mathcal{P}$	z_s	Significance		Reduced χ^2		
			$g_t(\theta_T)$	Γ	χ_{mod}^2	χ_{\times}^2	
5	[0.2, 0.5]	≤ 0.2	all	10	17	1.1	0.3
10	[0.2, 0.5]	≤ 0.2	all	9	12	1.4	0.5
20	[0.2, 0.5]	≤ 0.2	all	4	9	0.9	1.0
30	[0.2, 0.5]	≤ 0.2	all	3	6	0.7	1.0
10	[0.2, 0.5]	≤ 0.2	low	4	6	0.6	0.5
10	[0.2, 0.5]	≤ 0.2	high	8	11	1.4	0.6
10	[0.2, 0.4]	≤ 0.2	all	7	9	0.9	0.4
10	[0.4, 0.5]	≤ 0.2	all	5	10	1.2	0.6
10	[0.2, 0.5]	≥ 0.8	all	9	12	1.0	0.4

Table 1. Metrics of significance of detection of shear around troughs of radius θ_T selected from the galaxy field in the given redshift range z_T at the percentile threshold \mathcal{P} for sources in the indicated z_s bins. We list the signal-to-noise ratio of shear at the trough radius, $g_t(\theta_T)/\sigma_{g_t(\theta_T)}$, and of the optimally weighted linear combination of shears, Γ/σ_Γ . See description in Section 4.1.3 for details. The remaining columns show the reduced χ^2 of the residuals of model and measurement (cf. Section 4.3) and of cross-shears.

linear combination of observables yields even higher significances. Our detection of radial shear around underdensities on small scales of $\theta_T = 5 \dots 10'$ is of considerably higher significance than that of the most recent void lensing studies (Melchior et al. 2014; Clampitt & Jain 2014). On larger scales, significance decreases but is still comparable.

4.2 Trough-galaxy angular correlation

The lensing signal around troughs, studied in the previous sections, measures a weighted, projected version of the matter density field (cf. equation 4). Galaxies themselves also trace the matter field, yet with a different weighting. We have approximated the connection of galaxies to the matter density, so far, as being constant comoving density, deterministic, biased tracers. Measurements of the two-point correlation of trough positions with galaxies are complementary to trough lensing, sensitive to both the properties of the matter field and the details of the connection of galaxies and matter.

We measure the angular two-point correlation between trough positions and redMaGiC galaxies in the same redshift range of $z = 0.2 \dots 0.5$. Uncertainties are again estimated using jackknife resampling and are highly correlated between bins, as is common in clustering analyses.

Figure 8 shows results for the fiducial trough parameters, i.e. the trough catalogues also used in Fig. 4. The low galaxy count level inside the trough, due in part to the selection of regions of low matter density and to Poisson noise, steeply rises at the trough radius outside of which there is no Poisson contribution. Physical, smaller underdensities in the galaxy field are observed out to large radii. Section 3.3 discusses our modelling of the signal. Although only at moderate significance, there are indications of an increase of bias

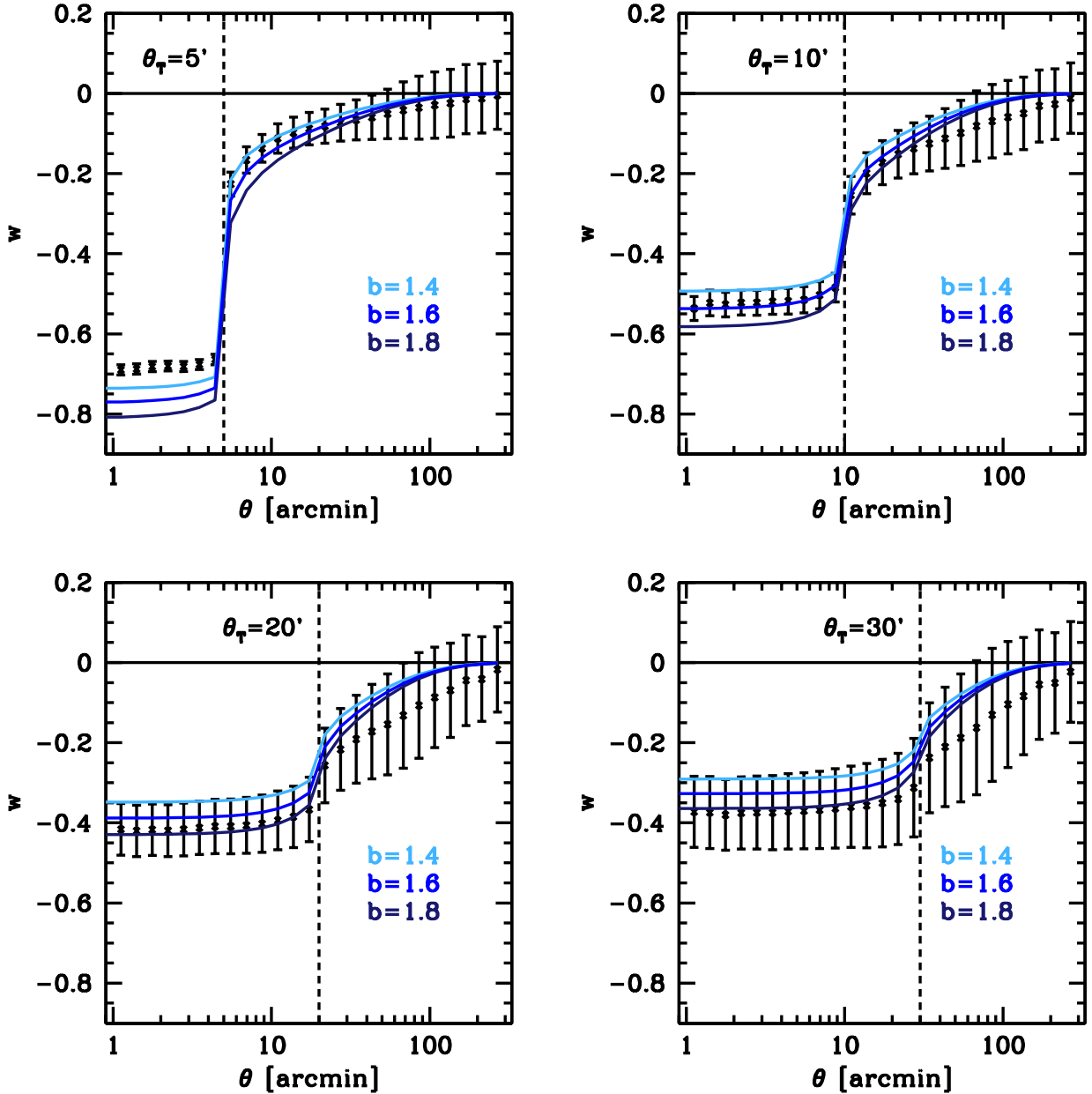


Figure 8. Angular two-point correlation of trough positions and redMaGiC galaxies in $z = 0.2 \dots 0.5$ for the same configurations as in Fig. 4. Shown are signal (black) and model predictions, for illustration for different values of the bias b (blue, cf. Section 3).

with trough radius, related to either a general scale or density dependence of bias or assembly bias (e.g. Wechsler et al. 2006).

4.3 Comparison to theory

We briefly compare our measurements to the model put forward in Section 3.

Our measurements of tangential shear around underdense troughs are consistent with the predictions at all scales and source and trough redshift configurations tested here. The reduced χ^2_{mod} of the residual of the data with respect to the $b = 1.6$ model are listed in Table 1 and consistent

with noise.. It is worth noting that the model is a good fit essentially without any free parameter. The only exception to this is the mild dependence on the assumed galaxy bias for the smallest scale $\theta_T = 5'$ considered here. This can be understood as an effect of the importance of Poisson noise relative to true variations in the matter density field as traced by the galaxies. On large scales where Poisson noise is subdominant, galaxies are dense tracers of the smoothed matter field. Independent of the details of the galaxy placement model, i.e. as long as galaxy and matter density are somewhat positively correlated, the selection of some percentile in galaxy count then yields an essentially equivalent selection in matter density.

The model also consistently predicts our measurements for the two-point correlation of troughs and galaxies and the shear around overdense cylinders. The only deviation from the prediction for these two probes is found for the smallest scale cylinders, where the amplitude of measured galaxy contrast inside the troughs is somewhat smaller and the measured shear around overdense cylinders is somewhat larger than predicted. Both observations indicate that at these scales, the linear bias of our galaxy placement model and/or the assumed Gaussianity of the matter field may be not completely valid.

The combination of these measurements therefore is sensitive to both the details of how galaxies follow matter in low and high density environments (e.g. a scale or density dependence of galaxy bias) and on cosmological parameters. These aspects will be studied in more detail in Friedrich et al. (in preparation).

5 CONCLUSIONS

We have presented the measurement of per-mille level radial gravitational shear of background galaxies and negative two-point correlation of foreground galaxies around underdense cylinders (troughs) in the foreground galaxy field in DES data from the Science Verification period.

- Our detection of radial shear around these projected underdense regions (cf. Section 4.1) is highly significant (above 10σ ; cf. Section 4.1.3), on the smallest projected scales and widest projection redshift range considered. This is a much higher significance than has been achieved with present data for the shear signal around three-dimensional voids.

- We develop a model for the shear profile (cf. Section 3), based on the assumption that galaxies are biased, Poissonian tracers of the Gaussian matter density field. The model predicts the lensing measurements consistently within the present level of uncertainty. It is interesting to note that on sufficiently large scales, the prediction is virtually independent of the details of the galaxy placement model, yet sensitive to cosmological parameters (cf. Friedrich et al., in preparation).

- Tomographic measurements that split the source sample or the redshift range used for the selection of troughs show consistent results. We note that the significance of radial shears strongly decreases for smaller trough redshift ranges, due to both the increased noise in galaxy counts and the variation of uncorrelated (overdense) structures along the line of sight in front or behind the trough cylinders.

- We measure the shear signals around underdense and overdense cylinders in galaxy count at the same percentile thresholds (cf. Section 4.1.2). On small scales we find indications for some deviation from our simple model predictions for the high density regions. On large scales, however, we recover the expected symmetry between radial and tangential shear for both cases.

- In addition to the shear signal, we measure and model the two-point correlation of galaxies from our tracer population around trough positions (cf. 4.2). While consistent with our prediction on sufficiently large scales, this probe is more sensitive to the details of how galaxies trace the matter and therefore complementary to the shear signal.

The statistical power of these measurements will strongly improve as larger data sets become available. We note, in particular, that the final survey area of DES will be ≈ 30 times larger at comparable or even better data quality, allowing very precise measurements of the trough lensing signal. With these better statistics, trough lensing will be a relevant probe of cosmology, not only in the sense of constraining parameters of a Λ CDM model. Also, the potential lack of screening mechanisms in underdense environments would influence the growth of negative density perturbations, with implications for constraining modified gravity models with these measurements.

On small scales, the details of how galaxies trace matter and the intrinsic distribution of the fields involved are likely to play a significant role for model predictions, and simulations in combination with progress on modeling will be required. Under these prerequisites, trough lensing measurements are a promising tool for probing the connection of galaxies and matter and gravity in the underdense Universe.

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REFERENCES

- Bartelmann M., Schneider P., 2001, *Physics Reports*, 340, 291
- Becker et al., on the arXiv on July 21, 2015
- Bonnett C., 2015, *Mon. Not. Roy. Astron. Soc.*, 449, 1043
- Bonnett et al., on the arXiv on July 21, 2015
- Brainerd T. G., Blandford R. D., Smail I., 1996, *ApJ*, 466, 623
- Brimioulle F., Seitz S., Lerchster M., Bender R., Snigula J., 2013, *Mon. Not. Roy. Astron. Soc.*, 432, 1046
- Cai Y.-C., Bernstein G., Sheth R. K., 2011, *Mon. Not. Roy. Astron. Soc.*, 412, 995
- Cai Y.-C., Padilla N., Li B., 2014, *ArXiv e-prints* 1410.1510
- Clampitt J., Cai Y.-C., Li B., 2013, *Mon. Not. Roy. Astron. Soc.*, 431, 749
- Clampitt J., Jain B., 2014, *ArXiv e-prints* 1404.1834
- Clampitt et al., in preparation
- DePoy D. L. et al., 2008, in *Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series*, Vol. 7014, *Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series*, p. 0
- Flaugher B., 2005, *International Journal of Modern Physics A*, 20, 3121
- Flaugher B. et al., 2015, *ArXiv e-prints* 1504.02900
- Fu L. et al., 2008, *A&A*, 479, 9
- Górski K. M., Hivon E., Banday A. J., Wandelt B. D., Hansen F. K., Reinecke M., Bartelmann M., 2005, *ApJ*, 622, 759
- Graff P., Feroz F., 2013, *SkyNet: Neural network training tool for machine learning in astronomy. Astrophysics Source Code Library*
- Gruen D., Bernstein G. M., Lam T. Y., Seitz S., 2011, *Mon. Not. Roy. Astron. Soc.*, 416, 1392
- Gruen D. et al., 2014, *Mon. Not. Roy. Astron. Soc.*, 442, 1507
- Hamaus N., Sutter P. M., Wandelt B. D., 2014a, *Physical Review Letters*, 112, 251302
- Hamaus N., Wandelt B. D., Sutter P. M., Lavaux G., Warren M. S., 2014b, *Physical Review Letters*, 112, 041304
- Hoekstra H., Mahdavi A., Babul A., Bildfell C., 2012, *Mon. Not. Roy. Astron. Soc.*, 427, 1298
- Hoekstra H., Yee H. K. C., Gladders M. D., 2004, *ApJ*, 606, 67
- Jarvis et al., on the arXiv on July 21, 2015
- Khoury J., Weltman A., 2004, *Phys. Rev. D*, 69, 044026
- Kilbinger M., Bonnett C., Coupon J., 2014, *athena: Tree code for second-order correlation functions. Astrophysics Source Code Library*
- Kilbinger M. et al., 2013, *Mon. Not. Roy. Astron. Soc.*, 430, 2200
- Krause E., Chang T.-C., Doré O., Umetsu K., 2013, *ApJ*, 762, L20
- Lam T. Y., Clampitt J., Cai Y.-C., Li B., 2014, *ArXiv e-prints* 1408.5338
- Leclercq F., Jasche J., Sutter P. M., Hamaus N., Wandelt B., 2015, 3, 47
- Limber D. N., 1954, *ApJ*, 119, 655
- Mandelbaum R., Seljak U., Kauffmann G., Hirata C. M., Brinkmann J., 2006, *Mon. Not. Roy. Astron. Soc.*, 368, 715
- Marrone D. P. et al., 2012, *ApJ*, 754, 119
- Marrone D. P. et al., 2009, *ApJ*, 701, L114
- Melchior P., Sutter P. M., Sheldon E. S., Krause E., Wandelt B. D., 2014, *Mon. Not. Roy. Astron. Soc.*, 440, 2922
- Peebles P. J. E., 1993, *Principles of Physical Cosmology. Princeton University Press*
- Rozo et al., on the arXiv on July 21, 2015
- Rykoff E. S. et al., 2014, *ApJ*, 785, 104
- Rykoff et al., in preparation
- Sánchez C. et al., 2014, *Mon. Not. Roy. Astron. Soc.*, 445, 1482
- Schneider P., Kochanek C., Wambsganss J., 2006, *Gravitational Lensing: Strong, Weak and Micro. Springer*
- Schneider P., van Waerbeke L., Kilbinger M., Mellier Y., 2002, *A&A*, 396, 1
- Schrabback T. et al., 2010, *A&A*, 516, A63
- Sheldon E. S. et al., 2004, *AJ*, 127, 2544
- Sheldon E. S. et al., 2009, *ApJ*, 703, 2217
- Smith R. E. et al., 2003, *Mon. Not. Roy. Astron. Soc.*, 341, 1311
- Sutter P. M., Lavaux G., Wandelt B. D., Weinberg D. H., 2012, *ApJ*, 761, 44
- Sutter P. M., Lavaux G., Wandelt B. D., Weinberg D. H., Warren M. S., Pisani A., 2014, *Mon. Not. Roy. Astron. Soc.*, 442, 3127
- The Dark Energy Survey Collaboration, 2005, *ArXiv e-prints* 0510346
- The Dark Energy Survey Collaboration et al., on the arXiv on July 21, 2015
- Tyson J. A., Wenk R. A., Valdes F., 1990, *ApJ*, 349, L1
- Umetsu K. et al., 2014, *ApJ*, 795, 163
- Vainshtein A., 1972, *Phys. Lett. B*, B39, 393
- van Uitert E., Hoekstra H., Velander M., Gilbank D. G., Gladders M. D., Yee H. K. C., 2011, *A&A*, 534, A14
- Velander M. et al., 2014, *Mon. Not. Roy. Astron. Soc.*, 437, 2111
- Vikram V. et al., 2015, *ArXiv e-prints* 1504.03002
- von der Linden A. et al., 2014, *Mon. Not. Roy. Astron. Soc.*, 439, 2

Wechsler R. H., Zentner A. R., Bullock J. S., Kravtsov A. V., Allgood B., 2006, ApJ, 652, 71
 Wittman D. M., Tyson J. A., Kirkman D., Dell'Antonio I., Bernstein G., 2000, Nat, 405, 143

APPENDIX A: CONDITIONAL PROBABILITIES

The conditional probability density of δ_T , given that N galaxies were found inside the radius θ_T , is given by

$$\begin{aligned} p(\delta_T|N) &= \frac{P(N|\delta_T)p(\delta_T)}{P(N)} \\ &= \frac{1}{\mathcal{N}} \frac{(\bar{N}[1+b\delta_T])^N}{N!} e^{-\bar{N}[1+b\delta_T]} \frac{1}{\sqrt{2\pi\sigma_T^2}} e^{-\frac{\delta_T^2}{2\sigma_T^2}}, \end{aligned} \quad (29)$$

where we have made the simple assumptions that galaxies trace matter with a constant bias b and that the variation of galaxy counts around the expectation value is given by the Poisson distribution. The normalisation constant gives the overall probability of finding N galaxies inside θ_T ,

$$\mathcal{N} = P(N). \quad (30)$$

In Appendix B, the trough variance σ_T^2 is derived from the 2D power spectrum of the projected matter contrast.

Note that in order to self-consistently define the biased Poisson model as explained above, equation 29 can only be valid for $\delta_T > -1/b$. Furthermore, one has to assume that

$$P(N|\delta_T \leq -1/b) = 0 \text{ for } N > 0. \quad (31)$$

As a consequence one also has

$$p(\delta_T|N) = 0 \text{ for } N > 0, \delta_T \leq -1/b. \quad (32)$$

The case $N = 0$, however, is more subtle. Here one has $P(N = 0|\delta_T \leq -1/b) = 1$, and hence

$$p(\delta_T|N = 0) = \frac{p(\delta_T)}{P(N = 0)} \text{ for } \delta_T \leq -1/b. \quad (33)$$

This also has to be considered when the probability $P(N = 0)$ is computed.

APPENDIX B: VARIANCE AND COVARIANCE OF CONVERGENCE AND δ_T

Let δ_i , $i = 1, 2$, be two line of sight projections of the matter density contrast δ , i.e.

$$\delta_i(\boldsymbol{\theta}) = \int_0^\infty d\chi q_i(\chi) \delta(\chi\boldsymbol{\theta}, \chi), \quad (34)$$

q_i being the weights of the projections (cf. Bartelmann & Schneider 2001). According to the Limber (1954) approximation, the 2D cross power spectrum of δ_1 and δ_2 is given by

$$C_{1,2}(\ell) = \int_0^\infty d\chi \frac{q_1(\chi) q_2(\chi)}{\chi^2} P_\delta\left(\frac{\ell}{\chi}, \chi\right). \quad (35)$$

Here, χ is the co-moving distance and a flat universe was assumed. Let A_i be annuli with minimal radius $\theta_{i,\min}$ and

maximal radius $\theta_{i,\max}$. The annulus-averaged versions of δ_i are given by

$$D_i(\boldsymbol{\theta}) = \frac{\int d^2\boldsymbol{\theta}' G_i(\boldsymbol{\theta} - \boldsymbol{\theta}') \delta_i(\boldsymbol{\theta}')}{\pi(\theta_{i+1,\max}^2 - \theta_{i,\max}^2)}, \quad (36)$$

where $G_i(\boldsymbol{\theta})$ is the top-hat filter corresponding to annulus A_i .

$\delta_i(\boldsymbol{\theta})$ can be expanded into spherical harmonics as follows:

$$\delta_i(\boldsymbol{\theta}, \phi) = \sum_{\ell, m} a_{i,\ell}^m Y_\ell^m(\boldsymbol{\theta}, \phi). \quad (37)$$

If δ_i is a homogeneous and isotropic random field then the coefficients a_ℓ^m satisfy the equation (cf. Peebles 1993)

$$\langle a_{i,\ell}^m a_{i,\ell'}^{-m'} \rangle = \delta_{\ell\ell'} \delta_{mm'} C_{i,\ell}, \quad (38)$$

where $C_{i,\ell}$ is the 2D power spectrum of δ_i .

Since the expectation values $\langle \delta_i \rangle$ vanish, the covariance $\langle D_1 D_2 \rangle$ can be computed as

$$\begin{aligned} \langle D_1 D_2 \rangle &= \int d\Omega_1 d\Omega_2 G_1(\boldsymbol{\theta}_1) G_2(\boldsymbol{\theta}_2) \langle \delta_1(\boldsymbol{\theta}_1) \delta_2(\boldsymbol{\theta}_2) \rangle \\ &= \sum_{\ell, m} \sum_{\ell', m'} \int d\Omega_1 d\Omega_2 G_1(\boldsymbol{\theta}_1) G_2(\boldsymbol{\theta}_2) \langle a_\ell^m a_{\ell'}^{-m'} \rangle \times \\ &\quad Y_\ell^m(\boldsymbol{\theta}_1) Y_{\ell'}^{-m'}(\boldsymbol{\theta}_2) \\ &= \sum_{\ell, m} C_\ell \int d\Omega_1 G_1(\boldsymbol{\theta}_1) Y_\ell^m(\boldsymbol{\theta}_1) \times \\ &\quad \int d\Omega_2 G_2(\boldsymbol{\theta}_2) Y_\ell^{-m}(\boldsymbol{\theta}_2) \\ &= \sum_{\ell, m} C_\ell G_{1,\ell}^{-m} G_{2,\ell}^m, \end{aligned} \quad (39)$$

where in the last step we used the relation (see e.g. Peebles 1993)

$$f_\ell^m = \int d\Omega f(\boldsymbol{\theta}) Y_\ell^m(\boldsymbol{\theta}). \quad (40)$$

The annuli and circles we will use as filters are isotropic, i.e. $G_i(\boldsymbol{\theta}, \phi) = G_i(\theta)$. Hence all coefficients $G_{i,\ell}^m$ vanish except for $G_{i,\ell}^0 =: G_{i,\ell}$. These are given by

$$\begin{aligned} G_{i,\ell} &= \int d\Omega G_i(\boldsymbol{\theta}) Y_\ell^0(\boldsymbol{\theta}) \\ &= \mathcal{N}_\ell \int_0^\pi d\theta \int_0^{2\pi} d\phi \sin(\theta) G_i(\theta) P_\ell(\cos(\theta)) \\ &= \frac{2\pi \mathcal{N}_\ell}{A_i} \int_{\theta_{i,\min}}^{\theta_{i,\max}} d\theta \sin(\theta) P_\ell(\cos(\theta)) \\ &= \frac{2\pi \mathcal{N}_\ell}{A_i} \int_{\cos \theta_{i,\max}}^{\cos \theta_{i,\min}} dx P_\ell(x). \end{aligned} \quad (41)$$

Here P_ℓ are the Legendre polynomials, A_i is the area of the annulus⁴ and \mathcal{N}_ℓ is a normalization factor given by

$$\mathcal{N}_\ell = \sqrt{\frac{2\ell+1}{4\pi}}. \quad (42)$$

⁴ The correct expression for the area is $A_i = 2\pi(\cos \theta_{i,\min} - \cos \theta_{i,\max})$.

The covariance then reads

$$\langle D_1 D_2 \rangle = \sum_{\ell} C_{\ell} G_{1,\ell} G_{2,\ell} . \quad (43)$$

Note that, using the equation

$$P_{\ell}(x) = \frac{1}{2\ell + 1} \frac{d}{dx} (P_{\ell+1}(x) - P_{\ell-1}(x)) , \quad (44)$$

one can simplify the $G_{i,\ell}$ to

$$G_{i,\ell} = \frac{2\pi\mathcal{N}_{\ell}}{(2\ell + 1)A_i} [P_{\ell+1}(x) - P_{\ell-1}(x)]_{\cos\theta_{\max}}^{\cos\theta_{\min}} . \quad (45)$$

The covariance of K_i and δ_T can then be computed by setting $\delta_1 = K_i$ and $\delta_2 = \delta_T$. The variance σ_T^2 is found by setting both δ_1 and δ_2 to δ_T .

AFFILIATIONS

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