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# Deuteron and triton production with high energy sulphur and lead beams

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**Abstract.** Proton and deuteron production has been observed in S+S and S+Pb collisions at 200 A·GeV and in Pb+Pb reactions at 158 A·GeV at the CERN SPS accelerator. For Pb+Pb triton production was also measured. The p and d spectra as well as the p and t spectra were observed in similar rapidity ranges and over similar ranges of transverse momenta per nucleon, making it possible to interpret the cross sections of the composite particles in terms of coalescence mechanisms. Volumes of homogeneity were extracted and compared to pion-pair HBT interferometry results. Special attention is given to the dependence on transverse mass, centrality and rapidity.

## 1 Introduction

The present paper reports on measurements of transverse momentum spectra of protons, deuterons and tritons from

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Pb+Pb collisions at 158 A·GeV/c beam momentum and for S+Pb and S+S at 200 A·GeV/c. The measurements were made in approximately the same range of transverse momenta per nucleon for all three species (p, d and t) and in similar rapidity intervals. The data therefore readily lend themselves to an analysis in terms of the nucleon [1–4] or fragment [5] coalescence models. Such an analysis leads to estimates of the reaction volume at freeze-out (i.e. at a time when strong interactions between the final state hadrons have ceased).

Deuterons and tritons are fairly large objects compared to simple hadrons and their binding energies (2.2 and 8.2 MeV, respectively) are small compared to freeze-out temperatures, which are on the order 100 MeV. These light clusters are therefore not expected to survive through the high density stages of the collision. The deuterons and tritons observed in the experiment are formed and emitted near freeze-out, and they mainly carry information about this late stage of the collision. This is evident from the

simple nucleon coalescence model [3,4], where the light cluster  $A(Z,N)$  is formed with an invariant multiplicity density in momentum space

$$E_A \frac{d^3 N_A}{dp_A^3} = B_A \left( E_p \frac{d^3 N_p}{dp_p^3} \right)^A, \quad (1)$$

where the cluster momentum  $p_A = Ap_p$  and  $p_p$  is the nucleon momentum, and it has been assumed that the neutron momentum density is proportional to the proton momentum density at freeze-out. The coalescence factor  $B_A$  can be derived from the measured invariant cross sections and it may be related to a freeze-out (source) volume  $V$  under conditions of thermodynamical equilibrium (thermal and chemical equilibrium),

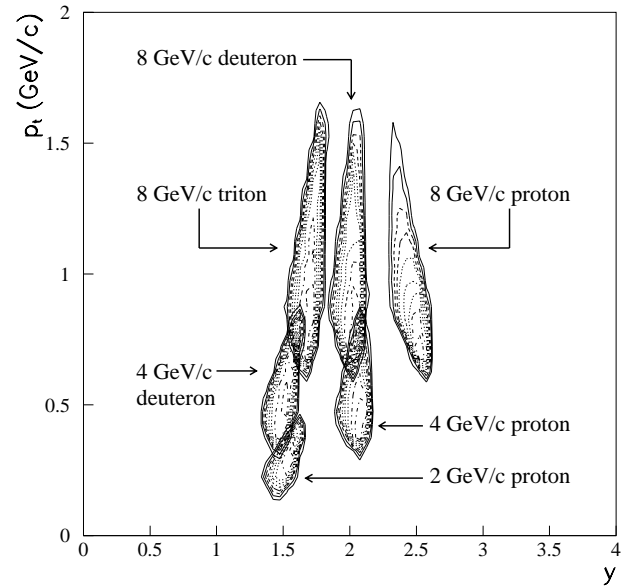
$$B_A = A \frac{2s_A + 1}{2^A} R_{np}^N \left( \frac{h^3}{m_p \gamma V} \right)^{A-1}. \quad (2)$$

Here  $R_{np}$  is the ratio of neutrons to protons participating in the collision,  $\gamma$  is the Lorentz factor related to the velocity  $\beta$  of the cluster  $A(Z,N)$  by  $\gamma = 1/\sqrt{1-\beta^2}$ . Equation (2) is valid only in the limit of the cluster binding energy being much smaller than the freeze-out temperature and for clusters that have no bound excited states.

The experiments presented here pay special attention to the transverse mass ( $m_t$ ) and rapidity dependence of the measured  $B_A$ -values. The observed  $m_t$ -dependence, in particular, shows that the simple thermodynamic expression (2) is not the proper model for an interpretation of the data; instead more complicated models that include collective flow explicitly [6–9] must be invoked. Under the conditions of special flow patterns Scheibl and Heinz [9] have derived an extension of (2) that allows the comparison of interaction volumes or rather “lengths (or volumes) of homogeneity” derived from Hanbury-Brown, Twiss (HBT) interferometry, with similar volumes derived from cluster formation cross sections. Such an analysis is presented for the Pb+Pb case at a nucleon transverse mass of  $\approx 1$  GeV, and good agreement between the volumes of homogeneity from interferometry and coalescence is demonstrated. The observed dependence of  $B_2$  on rapidity, however, disagrees with the model of [9]. Finally, an analysis of the triton formation by coalescence is presented, also in terms of the models of [6–9].

Measurements of deuteron coalescence in high energy heavy ion collisions have been reported previously both at AGS energies [20–24] from 10 to 14.6 A·GeV/c and at SPS energies [25–29] at 200 or 158 A·GeV/c. Of these, the AGS results of Si+A [20] and Au+Au [22] collisions as well as the SPS results of [25] are of special importance for the present study because they also deal with the systematics of deuteron production as function of rapidity, centrality, mass and transverse mass. The data reported in [26–28] are preliminary versions of part of the presently reported results.

The paper is organised as follows: Sects. 2 and 3 present the necessary experimental details and the data, respectively. In Sect. 4 we present the mass systematics of single particle inverse slopes, while Sect. 5 is devoted to the



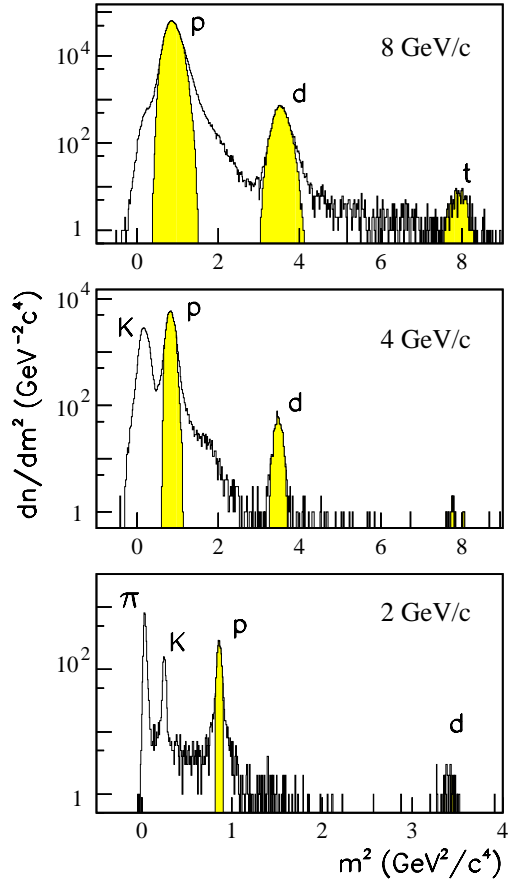
**Fig. 1.** The acceptance of the NA44 spectrometer at a polar angle of 129 mrad with respect to the beam direction. The acceptances are shown in  $p_t$  and  $y$  space for three different magnetic field settings corresponding to average momenta of 8, 4 and 2 GeV/c, for protons (all three settings), deuterons (8 and 4 GeV/c) and tritons (8 GeV/c)

derivation of the  $B_A$ -values from the measurements and a presentation of their systematic trends with  $m_t$ , rapidity and centrality. Section 6 deals with an interpretation in terms of the models including flow quoted above and the conclusions are presented in the last section.

## 2 Experiment and data analysis

The data were measured with the NA44 magnetic spectrometer [10] using 158 A·GeV/c  $^{208}\text{Pb}$  or 200 A·GeV/c  $^{32}\text{S}$  ions from the CERN SPS accelerator. For Pb+Pb reactions protons, deuterons and tritons were measured at magnetic field settings corresponding to mean momenta of 8 GeV/c, protons and deuterons at momenta of 4 GeV/c and finally protons at 2 GeV/c, all at a polar angle relative to the beam direction of 129 mrad. The corresponding acceptances in  $p_t - y$  (transverse momentum and rapidity) space are shown in Fig. 1, and are also quoted in Table 1, as  $m_t - m$  and  $y$  intervals ( $m_t$  is the transverse mass  $m_t = (p_t^2 + m^2)^{1/2}$  and  $m$  the mass). It may be seen that the deuteron and proton data are in identical rapidity intervals while the tritons (8 GeV/c) are in an interval that lies 0.1 units higher than the 2 GeV/c protons. In the coalescence analysis to follow, this difference has been ignored. The quality of the particle identification made from the three time-of-flight measurements is demonstrated in Fig. 2.

The main trigger was provided by a scintillator ( $T_0$ ) placed immediately behind the target, covering pseudo rapidities from 1.3 to 3.5. The offline centrality cuts were made from the additional information from a silicon-pad

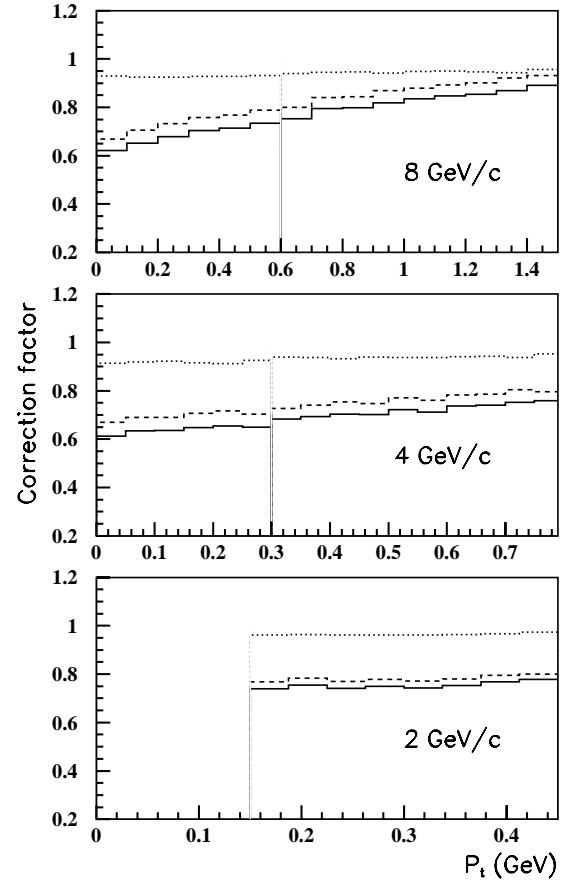


**Fig. 2.** Spectra of number of counts per unit of mass squared plotted against the mass squared. The particle identification for protons, deuterons and tritons are shown as shaded areas, corresponding to Gaussian fits. No global background subtractions were employed

multiplicity detector placed after  $T_0$  [10]. The cross section corresponding to the 20% of the reactions with highest charged particle multiplicity, was  $\sigma_{trig} \approx 150 \text{ fm}^2$ . A second level veto, for the rejection of pions and most of the kaons, was imposed on events with particles that fired the threshold Cherenkov counters in the spectrometer arm. The corresponding efficiency correction was measured from spectrometer runs with the Cherenkov veto turned off. All cuts in the data analysis were mimicked in the GEANT Monte Carlo simulation of the experiment and the corresponding efficiency corrections were applied to the data.

The Sulphur beam had a momentum of 200 A-GeV/c and the data were measured at the 8 GeV/c setting for deuterons and at 4 GeV/c for protons. The nominal spectrometer angles were 44 mrad and 129 mrad, the rapidity interval from 1.9 to 2.3 and the centrality 9% for S+S and 11% for S+Pb. The corresponding trigger cross sections were approximately  $19 \text{ fm}^2$  for S+S and  $44 \text{ fm}^2$  for S+Pb. The data analysis procedures were the same as used for the Pb beam measurements.

A special correction must be applied to the measured proton spectra, because the NA44 spectrometer does not

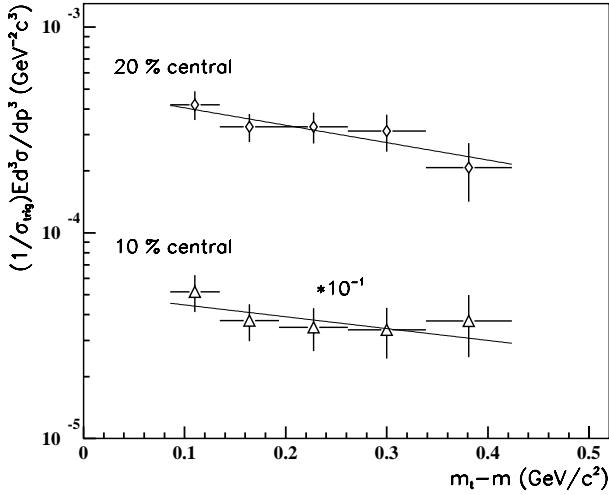


**Fig. 3.** The correction factor  $C(p_t)$  from (3), plotted against transverse momentum for the three magnetic field settings. The fully drawn curves incorporate both the  $\Lambda$  and  $\Sigma$  corrections, the dashed curves represent the corrections for  $\Lambda$  decays only and the dotted curves  $\Sigma$  decays only

measure the vertex from where the particles emerge. A number of protons originate as decay products from hyperons, e.g. from the decay  $\Lambda \rightarrow p + \pi^-$ , where the  $\Lambda$  in turn may have been produced from other hyperons, typically via  $\Sigma^0 \rightarrow \Lambda + \gamma$ , or from proton decay of other hyperons. The “feed down” corrections,  $C(p_t)$ , were calculated from the GEANT Monte Carlo simulation of the NA44 experiment, with particle distributions from the RQMD 1.08 [11] event generator as input,

$$C(p_t) = \frac{N_p(p_t)}{N_p(p_t) + N_\Lambda(p_t) + N_{\Sigma^+}(p_t)}, \quad (3)$$

where  $N_p$ ,  $N_\Lambda$  and  $N_{\Sigma^+}$  are the number of reconstructed direct protons, protons from  $\Lambda + \Sigma^0$  decays and protons from  $\Sigma^+$  decays, respectively.  $C(p_t)$  for the Pb+Pb case is shown in Fig. 3 for the three momentum settings used, plotted versus  $p_t$ . The figure shows that the correction varies from 10% to 30% and that the high momentum setting exhibits a distinct  $p_t$  dependence. The RQMD model gives a fair account of the  $\Lambda$  cross sections measured by the NA49 and WA97 experiments [12,13] and the systematic errors introduced by the corrections of (3) are considerably smaller than the corrections themselves.



**Fig. 4.** Triton spectra from Pb+Pb interactions plotted as invariant triply differentiated multiplicity against transverse mass minus mass. The curves are exponential fits of the form shown in (4). The fitted parameters are given in Table 1. The centrality cuts are described in the text. Only statistical uncertainties are shown

### 3 Data and results

#### 3.1 Pb+Pb

The invariant differential multiplicities  $Ed^3N/dp^3$  for tritons, at the 8 GeV/c setting of the spectrometer are shown in Fig. 4 as function of  $m_t - m$ . Data are shown for the on-line multiplicity cut at 20% of the inelastic cross section, and in addition for an off-line multiplicity cut at 10%. The systematic errors on the multiplicities derive mainly from two sources, the trigger cross section and the live-time of the data acquisition system. For the data of Fig. 4, the total systematic error is estimated to be  $\approx 10\%$ .

The curves shown in the figure represent exponential fits to the data points of the functional form

$$Ed^3N/dp^3 = \frac{1}{\sigma_{trig}} E \frac{d^3\sigma}{dp^3} = A \exp(-(m_t - m)/T) \quad (4)$$

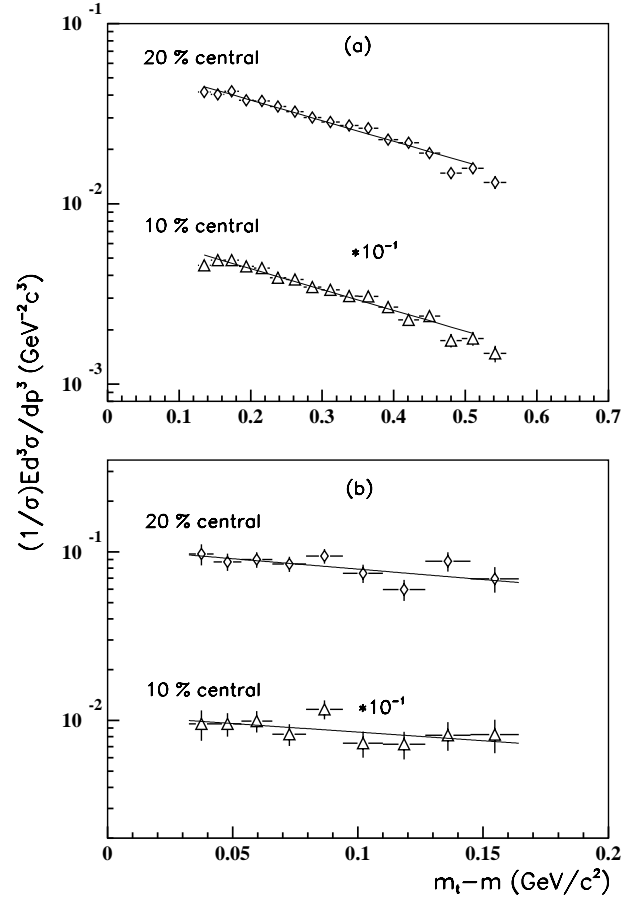
with  $A$  and  $T$  as the fitting parameters.  $T$  is referred to as the inverse slope parameter. The  $m_t - m$  interval used for the fit corresponds with the end points of the fit line shown in the figure.

Figures 5a and b depict the deuteron transverse mass spectra, (a) for the 8 GeV/c field setting and (b) for the 4 GeV/c setting. The exponential fits are shown in the same manner as for the tritons.

The proton spectra, corrected for “feed down”, (3), are shown in Figs. 6a–c for the three different field settings employed and for the two different cuts on charged multiplicity, 20% and 10%. The exponential curves have the same meaning as for tritons.

The rapidity density  $dn/dy$  may be obtained from the fitted exponential of (4) by

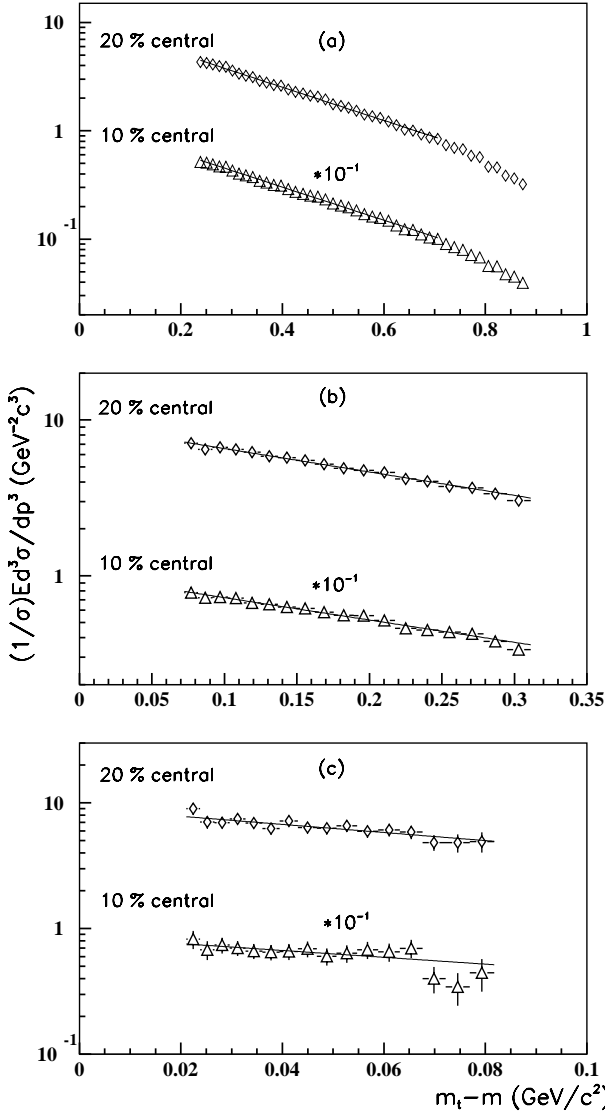
$$\frac{dn}{dy} = 2\pi \int_m^\infty \frac{1}{\sigma_{trig}} E \frac{d^3\sigma}{dp^3} m_t dm_t = 2\pi AT(T + m). \quad (5)$$



**Fig. 5a,b.** Deuteron spectra from Pb+Pb collisions. **a** is for a magnetic field setting corresponding to a mean momentum of 8 GeV/c and a rapidity interval from 1.8 to 2.2, while **b** corresponds to a mean momentum of 4 GeV/c and rapidities from 1.4 to 1.7. Other details are as for Fig. 4

The values of  $dn/dy$  and  $T$  are collected in Table 1, which summarises the single particle results for the p, d and t spectra. The uncertainties listed in the table are statistical only. The  $dn/dy$  values represent extrapolations into unmeasured regions under the explicit assumption of exponential shape. Hence a strict systematic error cannot be assigned, but it is at least 10% from the normalisation and efficiency corrections as discussed above. For protons it is increased on account of the feed down corrections to about 15%. For the tritons, the  $m_t$  interval is very narrow and close to the rest mass, so the uncertainties on both  $dn/dy$  and the inverse slope become large and asymmetric. For the 10% centrality case the statistical uncertainty on  $dn/dy$  is larger than 100% and hence no  $dn/dy$  is quoted.

The inverse slope parameters,  $T$ , depend on which range of the data is fitted, because the data do not exactly follow the assumed functional form. For the proton data at 8 and 4 GeV/c the variations with fit range are larger than the statistical errors, typically 10–20 MeV. The deuteron spectra have similar systematic errors. For the 2 GeV protons the fitting range is critical and the  $m_t - m$  interval is close to zero, where the proton spectra often

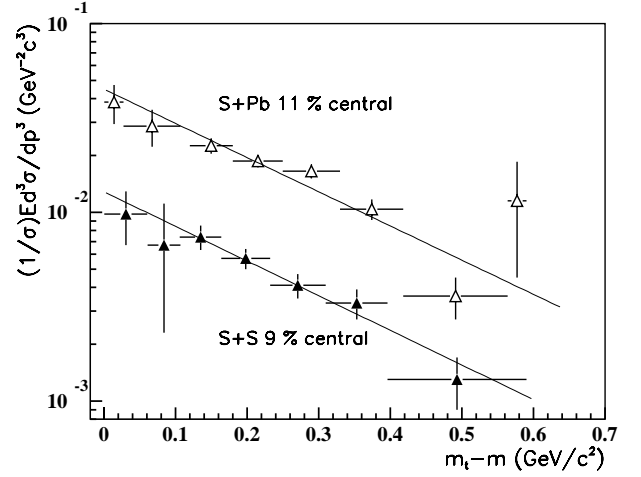


**Fig. 6a–c.** Proton spectra from Pb+Pb reactions. **a** is for a mean momentum of 8 GeV/c and rapidities from 2.3 to 2.6, **b** corresponds to a mean momentum of 4 GeV/c and a rapidity interval from 1.8 to 2.2, while **c** is for 2 GeV/c and rapidities between 1.4 and 1.7. Other details are as for Fig. 4

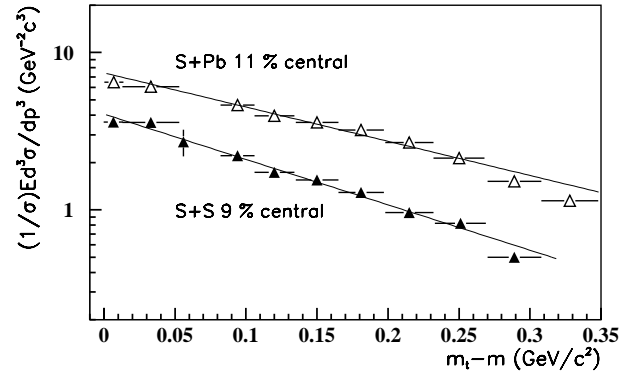
deviate from the exponential shape. Even if the statistical errors are large, the systematic errors may dominate. The extrapolated  $dn/dy$  values in this case are not representative and are not quoted in Table 1. In the triton and 2 GeV/c proton cases, the statistical uncertainties have been assigned from  $\chi^2$  contours and correspond to an increase of one unit in  $\chi^2$ .

### 3.2 S+Pb and S+S

The deuteron and proton spectra from the S+S and S+Pb collisions are shown in Figs. 7 and 8, respectively. The exponential fits are shown in the same way as for the Pb+Pb data. The field settings were 8 GeV/c for the deuterons



**Fig. 7.** Deuteron spectra from S+Pb and S+S collisions at 200 A-GeV/c beam momentum. Details are as for Fig. 4. See also Table 1 and the text



**Fig. 8.** Proton spectra from S+Pb and S+S collisions at 200 A-GeV/c beam momentum. Details are as for Fig. 4. See also Table 1 and the text

and 4 GeV/c for the protons and the rapidity interval covered from 1.9 to 2.3. The numerical results obtained from the exponential fits are shown in Table 1. The systematic uncertainties are similar to those quoted for the 8 GeV/c deuteron and 4 GeV/c proton results for Pb+Pb, i.e. 10% for deuteron  $dn/dy$  and  $\approx 15\%$  for protons and 10-20 MeV on the inverse slope parameters.

## 4 Mass systematics of slope parameters

It has previously [14, 25] been pointed out that the inverse slope parameters for Pb+Pb collisions depend systematically on the mass of the emitted particle: the inverse slope increases with increasing mass. This observation was interpreted as being caused by a collective transverse flow. The present measurements extend the mass range used in [14] by deuterons and tritons. The previous  $\pi$  and K meson results are shown in Fig. 9 as filled triangles together with the present results for 20% centrality (filled circles). The  $\pi$  and K results are for a centrality of 6.4%. The present p and d data for Pb+Pb collisions were also

**Table 1.** Single particle results. Errors are statistical only

Reaction	Field setting	Centrality	A	Rapidity	$m_t - m$ range	T (MeV)	$dn/dy$
Pb+Pb	8 GeV/c	20%	p	2.3-2.6	0.23-0.88	283±2	22.3±0.3
		10%	p	2.3-2.6	0.23-0.88	284±2	26.9±0.3
	4 GeV/c	20%	p	1.8-2.2	0.08-0.32	288±6	20.6±0.6
		10%	p	1.8-2.2	0.08-0.31	302±9	23.8±0.9
	2 GeV/c	20%	p	1.4-1.7	0.02-0.08	128±29	
		10%	p	1.4-1.7	0.02-0.08	114±33	
Pb+Pb	8 GeV/c	20%	d	1.8-2.2	0.13-0.56	379±13	0.34±0.02
		10%	d	1.8-2.2	0.13-0.56	376±17	0.39±0.02
	4 GeV/c	20%	d	1.4-1.7	0.03-0.16	350±149	0.51±0.23
		10%	d	1.4-1.7	0.03-0.16	425±286	0.66±0.46
Pb+Pb	8 GeV/c	20%	t	1.5-1.8	0.08-0.42	512 <sup>+511</sup> <sub>-179</sub>	0.0052 <sup>+0.0047</sup> <sub>-0.0013</sub>
		10%	t	1.5-1.8	0.08-0.42	747 <sup>+∞</sup> <sub>-380</sub>	
S+Pb	4 GeV/c	11%	p	1.9-2.3	0.01-0.32	200±4	10.6±0.1
	8 GeV/c	11%	d	1.9-2.3	0.02-0.58	240±20	0.14±0.01
S+S	4 GeV/c	9%	p	1.9-2.3	0.01-0.29	151±3	4.2±0.1
	8 GeV/c	9%	d	1.9-2.3	0.02-0.48	236±33	0.040±0.003

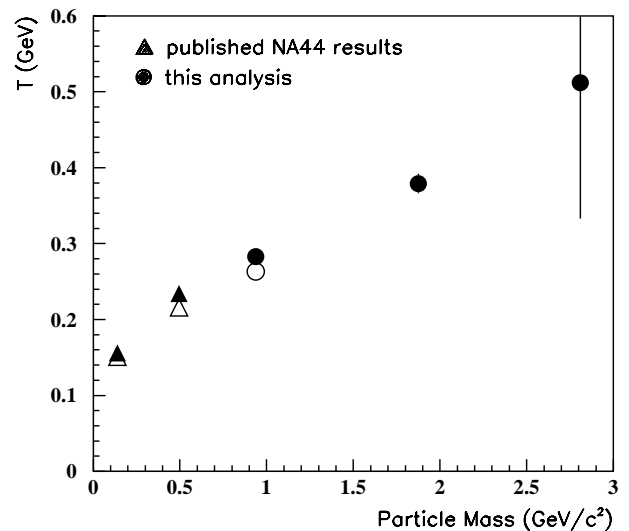
analysed with 5 and 2% centrality cuts, but no significant variation with centrality was observed for the inverse slope parameters. The K and  $\pi$  inverse slopes have also been measured at other centralities [15] without revealing any systematic changes. Inverse slopes, however, do depend sensitively on rapidity. The open points for  $\pi$ , K and p in Fig. 9 have been corrected by means of RQMD calculations to a common rapidity interval of  $1.6 < y < 2.0$ , corrections that are barely outside the statistical errors. The proton slopes are from spectra corrected for feed down, which is different from the proton slopes presented in [14] and [16].

The previous observation of inverse slope parameters as increasing with increasing mass is further supported by the present data.

## 5 The coalescence analysis

The prescription (1) has been used to derive  $B_2$  and  $B_3$  values from the spectra in Figs. 4–8. Figure 10 shows Pb+Pb  $B_2$ -values versus deuteron  $m_t - m$  for the rapidity interval from 1.8 to 2.2 (a and b), corresponding to deuterons from the 8 GeV/c and protons from the 4 GeV/c field settings, while Figs. 10c and d depict  $B_2$  values from Pb+Pb collisions at the 4 GeV/c deuteron setting and the 2 GeV/c proton setting in the rapidity interval  $1.4 < y < 1.7$ . The Pb+Pb  $B_3$  from tritons at the 8 GeV/c and protons at 2 GeV/c settings in the rapidity interval 1.5 to 1.8 are presented in Fig. 11 and the S+S and S+Pb  $B_2$ -values are shown in Figs. 12. For all three figures the cluster  $m_t - m$  was used as the abscissa.

The figures demonstrate that the  $B$ -values in general depend on  $m_t$ , a feature to be expected because of the differences in inverse slopes between the p, d and t spectra

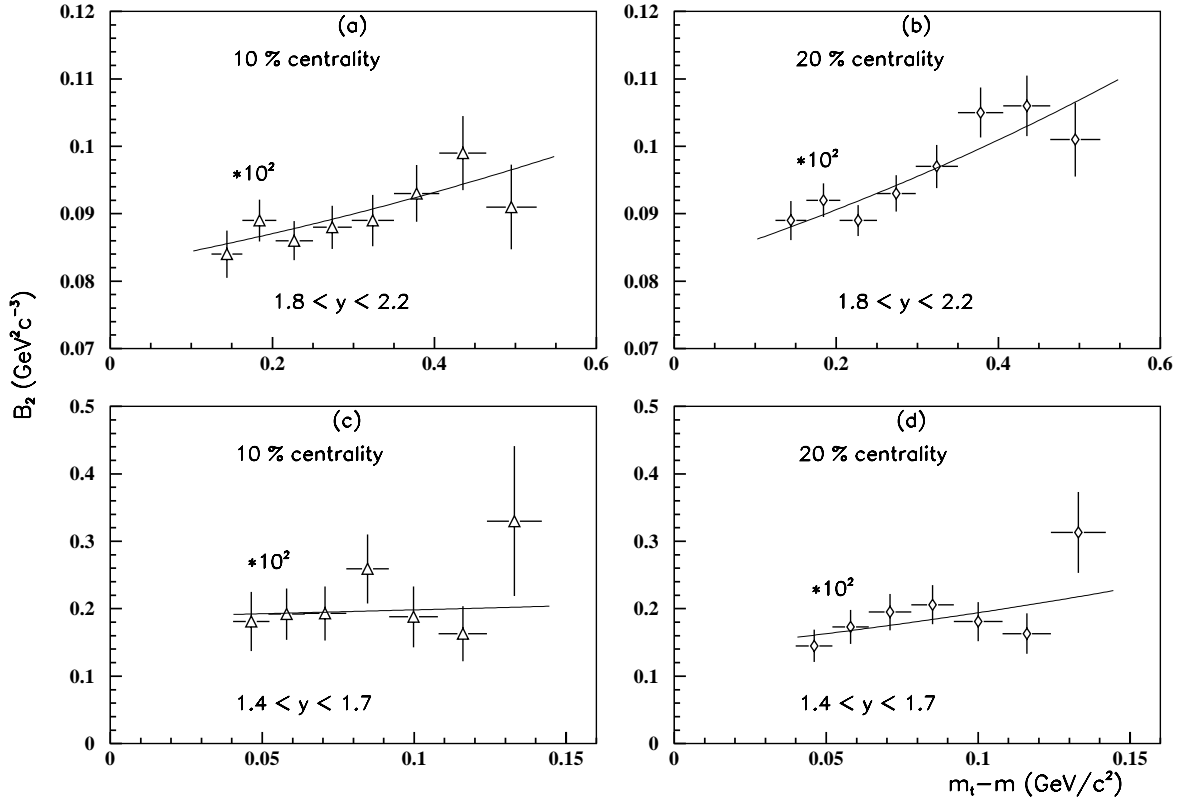


**Fig. 9.** Inverse slope parameters  $T$  (see (4)) as a function of particle mass. The data for pions and kaons are from [14] while the proton, deuteron and triton results are from this work. Open points are data corrected by means of RQMD to a rapidity interval of  $1.6 < y < 2.0$

(see also [22, 25]). To the extent that the single particle spectra can be represented by an exponential function in  $m_t$ , the  $B$ -values depend exponentially on the transverse mass of the cluster  $M_t$ ,

$$B_A \propto \exp(M_t(1/T_p - 1/T_A)), \quad (6)$$

where  $T_p$  is the inverse slope of the proton spectrum and  $T_A$  the inverse slope for the cluster spectrum. (The notation  $M_t$  is used from now on for the transverse mass of the cluster, while  $m_t$  denotes the same quantity for a nu-



**Fig. 10a–d.**  $B_2$  values from Pb+Pb reaction plotted versus deuteron  $m_t - m$ . The two top frames **a** and **b** are from 8 GeV/c deuteron and 4 GeV/c proton data. All  $B_2$  values have been multiplied by a factor  $10^2$ . The curves through the measured points represent fits to (10) and the fit parameters are given in Table 3. Only statistical uncertainties are shown. The two lower frames, **c** and **d**, are from 4 GeV/c deuteron and 2 GeV/c proton data. All other details are as for the two top frames

cleon; similarly  $M$  and  $m$  denote the cluster and nucleon rest masses, respectively.) The coalescence parameters are summarised in Table 2 in two ways: For each rapidity interval the weighted average  $B_A$  is given for the  $M_t - M$  range of the measurement (see Figs. 10–12); in addition the parameters of exponential fits to the functional form are given in the two right hand columns. Note that both  $a$  and  $b$  were allowed to vary in the fitting procedure, so  $b$  does not necessarily equal the difference in inverse slope values from Table 1.

$$B_A = a \exp(b(M_t - M)) \quad (7)$$

It appears from the average  $B_A$ -values in the table, that the dependence on centrality is weak. In most cases  $B_A$  increases with increasing  $M_t$ . This (see (6)) reflects that  $T_A > T_p$  in accordance with the systematics of Sect. 4. In the two cases, where an increase with  $m_t - m$  is not observed (Pb+Pb deuterons for  $1.4 < y < 1.7$  and S+Pb deuterons  $1.9 < y < 2.3$ ) the  $B_2$  values do not vary with  $m_t - m$ .

In the thermal limit, where the interpretation of  $B$ -values in terms of (2) becomes valid, both  $M_t$  and rapidity dependences become explicit. In the Boltzmann limit one has

$$B_A \propto \frac{1}{(M_t \cosh y)^{A-1}}, \quad (8)$$

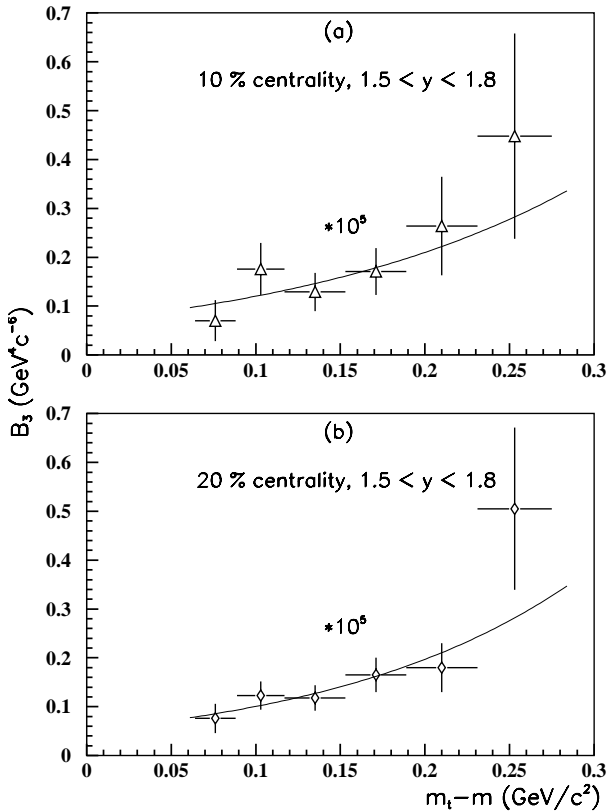
where  $y$  is the common rapidity of protons and cluster in the source system of reference. The general trend with  $M_t$  from the inverse slope parameters in Table 1 and from Figs. 10–12 is an increase in  $B_A$  with increasing  $M_t$  rather than a decrease as suggested by (8). The fit parameters  $b$  quoted in Table 2 are positive in all cases, but only for Pb+Pb in the rapidity interval from 1.8 to 2.2 and for S+S are they positive by two standard deviations.

It appears from Table 2 that the average values of  $B_2$  for the Pb+Pb system depend on rapidity: the  $B_2$ -value doubles from the 1.8-2.2 rapidity interval to the 1.4-1.7 interval. Equation (8) predicts a decrease by a factor of  $\approx 1.5$  if we take the source rest system to be the center of mass system for Pb+Pb at  $y=2.91$ .

## 6 Discussion

In the Au+Au experiment at 11.6 A·GeV/c reported in [22] the  $B_2$ -values were also observed systematically to increase with  $m_t$  and to increase in magnitude towards mid-rapidity. The Si+A experiment at 14.6 A·GeV/c shows that  $B_2$  decreases with target mass, averaged over  $m_t$ . The SPS Pb+Pb experiment [25] again demonstrates that  $B_2$  increases with increasing  $m_t$ , here for the rapidity interval  $2.0 < y < 2.5$ . For this rapidity interval the  $B_2$ -value averaged over the same  $m_t - m$  range as used in the present ex-



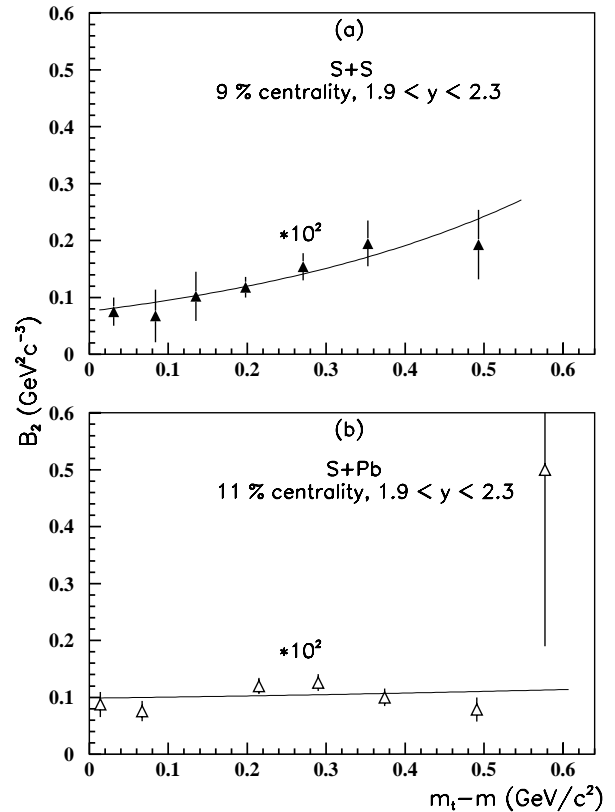


**Fig. 11a,b.**  $B_3$  values from Pb+Pb collisions plotted versus triton  $m_t - m$ . The results are from 8 GeV/c tritons and 2 GeV/c protons. All data have been multiplied by a factor of  $10^5$ . The curves are from fits to (13) as explained in the text and the fit parameters are stated in Table 3. All other details are as in Fig. 10

periment is  $5.7 \pm 1.5 \text{ GeV}^2 \text{c}^{-3}$ , i.e. somewhat smaller than the present value of  $8.8 \pm 0.1 \text{ GeV}^2 \text{c}^{-3}$  for  $1.8 < y < 2.2$ . The increase in  $B_2$  with increasing  $m_t$  apparently is a general phenomenon, whereas the rapidity dependence at 11.6 A·GeV/c is in the opposite direction of the observations for Pb+Pb at 158 A·GeV/c.

It does not seem reasonable to interpret the  $B_A$ -values in terms of the thermal expression of (2) in view of the systematics of the data presented in the previous section. In general one should expect the dynamics of the source expansion to be important for the coalescence mechanism, and the following discussion is therefore based on models that explicitly consider rapid source expansion.

The models of Polleri et al. and of Scheibl and Heinz [8,9] incorporate a fast “collective” expansion and a local thermodynamic equilibrium, so the observed inverse slopes in the transverse spectra (Fig.9) are interpreted as an apparent temperature, comprised of a local temperature and the superimposed “collective” motion. The coalescence process is described in the local equilibrium system and it is shown by Scheibl and Heinz that the observed nucleon and cluster spectra as well as the  $B_A$ -values can be understood in terms of the same lengths of homogeneity that can be extracted from HBT interferometry.



**Fig. 12a,b.**  $B_2$  values from S+S and S+Pb interactions at 200 A·GeV/c beam momentum. All details are as for Fig. 10

The term “lengths of homogeneity”, used in [9], stands for the radius parameters extracted from interferometry; the term “volume of homogeneity” is used for a product of three such radius parameters, as defined more precisely in (9) below.

The model of Polleri et al. only deals with the transverse motion, while Scheibl and Heinz also include the motion in the beam direction.

A preliminary version of the Pb+Pb data presented in Figs.6 and 5 for 20% centrality and rapidity interval 1.8-2.2 were used by Polleri et al. [8] to calculate a set of dimensionless transverse density functions, one for each “local” temperature assumed. The coalescence condition of proportionality between the deuteron and the square of the proton densities, was then used to construct a collective transverse velocity profile. The various combinations of “local” temperature and density profile all fit the experimental spectra about equally well. In the thesis of Polleri [7] the corresponding triton results are also calculated, assuming two competing routes, namely a direct “triple” coalescence  $p+n+n \rightarrow t$  and a sequential coalescence  $p+n+n \rightarrow d+n \rightarrow t$ . The predicted triton spectra again fit the data for all the density and temperature combinations used from the p and d spectra. Without the sequential route, however, the triton cross section is severely underpredicted.

If the value of the local temperature is taken to be 130 MeV (see e.g. [9,15]) the result of the analysis in [8]

**Table 2.**  $B_A$ -values in  $(\text{GeV}^2\text{c}^{-3})^{A-1}$ 

Reaction	A	Rapidity	Centrality %	$B_A$		
				$\cdot 10^{-4}$	a $\cdot 10^{-4}$	b
Pb+Pb	2	1.8-2.2	20	9.35±0.11	8.1±0.3	0.55±0.29
Pb+Pb		1.8-2.2	10	8.84±0.13	8.1±0.4	0.33±0.15
Pb+Pb		1.4-1.7	20	18.00±1.10	13.7±3.2	3.50±2.70
Pb+Pb		1.4-1.7	10	19.60±1.70	18.7±6.7	0.56±4.10
Pb+Pb	3	1.5-1.8	20	0.013±0.002	0.0048±0.0027	7.1±3.4
Pb+Pb		1.5-1.8	10	0.014±0.002	0.0047±0.0013	8.2±2.4
S+Pb	2	1.9-2.3	10	10.30±0.70	9.8±1.2	0.20±0.36
S+S	2	1.9-2.3	9	12.10±1.10	7.5±1.5	2.34±0.72

may be summarised as a transverse velocity profile and a local proton (or deuteron) density as function of transverse distance. The root mean square velocity is  $\approx 0.4c$  and the root mean square transverse radius  $\approx 8.1$  fm (interpolated from Table 1 of [8]). The transverse density profile is more box-like than Gaussian in shape. An important further test of this model would be a consistent description of the present  $B_2$  results in the rapidity interval from 1.4-1.7.

The model of Scheibl and Heinz [9] assumes a boxlike transverse density profile and results in a connection between the  $B_2$ -value and a volume of homogeneity given by

$$B_2 = e^{\frac{N(\mu_n - \mu_p)}{T}} \frac{3\pi^{3/2} \langle C_d \rangle \hbar^3}{M_t R_\perp^2 (M_t) R_\parallel (M_t)} e^{(M_t - M)(1/T_p - 1/T_d)}, \quad (9)$$

where  $\mu$  are the chemical potentials for protons and neutrons,  $\langle C_d \rangle$  is a quantum mechanical correction factor related to the deuteron internal structure and  $R_\perp$  and  $R_\parallel$  denote lengths of homogeneity, while the product  $R_\perp^2 R_\parallel$  is the volume of homogeneity mentioned above. The formula above combines equations (6.4) and (6.5) in [9], where it should be noted that the transverse and rest masses in (9) refer to the deuteron, while the nucleon masses were used in [9].

The  $B_2$ -value for antideuterons has been measured [17] in Pb+Pb collisions at 10% centrality for a rapidity interval from 1.9 to 2.1 and an antideuteron  $M_t - M$  interval from 0.16 to 0.53 GeV with a value of  $(4.4 \pm 1.3 \pm 1.8) 10^{-4} \text{ GeV}^2\text{c}^{-3}$  averaged over  $M_t$ . The second quoted uncertainty represents an estimate of the systematic uncertainty of the correction for the contribution from weak decays to the antiproton yield. The comparable deuteron  $B_2$ -value from Table 2 is  $(8.8 \pm 0.1 \pm 0.9) 10^{-4} \text{ GeV}^2\text{c}^{-3}$ . With a ratio  $B_2/B_{\bar{2}} \approx 2$ , the difference between the chemical potentials is  $\mu_n - \mu_p = 0.00036$  GeV with a near 100% uncertainty. In this estimate the ‘‘local’’ temperature was set to 130 MeV and neutron number  $N=126$  and the slope factors were assumed to be equal for particles and antiparticles. It is noted that, if a 5 to 10% centrality cut in the  $\bar{d}$  case had been used instead of 0 to 10%, the  $B_2$ -values for deuterons and antideuterons would have been very close ( $9.8 \cdot 10^{-4}$  for antideuterons and no change for deuterons). The data are thus in agreement with  $\mu_p = \mu_n$  in (9).

Equation (9) was used to derive volumes of homogeneity in the form of  $R_\perp^2 R_\parallel$  values in  $\text{fm}^3$ . The expression

$$B_2 = \alpha \frac{1}{M_t} \exp((M_t - M)\delta) \quad (10)$$

was fitted to the  $B_2$ -values of Figs. 10 and 12 with  $\alpha$  and  $\delta$  as the fit parameters and  $M_t$  and  $M$  referring to the deuteron. (The fits are shown in the figures in comparison with the data). The volume of homogeneity is then

$$R_\perp^2 R_\parallel = \frac{0.1283 \langle C_d \rangle}{\alpha}. \quad (11)$$

The  $\langle C_d \rangle$  is 0.80 for the Pb+Pb case (see [9]) and for the sulphur beam cases it was roughly estimated from (4.12) of [9] by scaling the  $R$ -values for Pb+Pb in the quoted reference to S+Pb and S+S with the values of Table 4 in Bearden et al. [18]. The  $\langle C_d \rangle$  are given in the table, as are the volumes of homogeneity from HBT results for Pb+Pb from NA44 [10] and NA49 [19], the latter as quoted in [9]. The HBT-values are from pion data at  $m_t$ -values near 1 GeV and from higher rapidities than the present coalescence data.

The main result from the analysis of Table 3, is that the present Pb+Pb data in the rapidity range from 1.8-2.2 yield volumes of homogeneity in near agreement with the HBT results but give lower values for the more backward rapidity interval from 1.4-1.7. The HBT pion-pair  $m_t$  range used for the comparison is important. The fit parameter  $\alpha$  used to determine the value of the volume of homogeneity corresponds to setting  $M_t = M$ , i.e. corresponds to a nucleon  $m_t$  value of 0.94 GeV. One should use a similar pion-pair  $m_t$  value in the HBT case (see also [9]). The HBT results used in Table 3 are for  $m_t$  values near the nucleon mass. If lower HBT  $m_t$  values are used in the comparison, the HBT volumes become considerably larger and the agreement disappears.

The relation between  $B_3$  and the volume of homogeneity, corresponding to (9) is

$$B_3 = \frac{18\pi^3 \langle C_t \rangle \hbar^6}{\sqrt{3} M_t^2 R_\perp^4 R_\parallel^2} e^{(M_t - M)(1/T_p - 1/T_t)} \quad (12)$$

with the proton and neutron chemical potentials set equal to one another. The inverse slope parameters for the tritons  $T_t$  are ill defined, but they are considerably larger

**Table 3.** Volumes of homogeneity

Reaction	A	Rapidity	Centrality %	$\alpha$ $\cdot 10^{-4}$	$\delta$	$\langle C_A \rangle$	$R_{\perp}^2 R_{\parallel}$ fm <sup>3</sup>
Pb+Pb	d	1.8-2.2	20	15.4±0.5	1.0±0.1	0.80	68±2
Pb+Pb	d	1.8-2.2	10	15.4±0.7	0.8±0.2	0.80	67±3
Pb+Pb	d	1.4-1.7	20	25.7±6.0	4.0±2.7	0.80	40±9
Pb+Pb	d	1.4-1.7	10	35.1±12.5	1.1±4.2	0.80	29±10
S+Pb	d	1.9-2.3	11	18.5±2.6	0.7±0.5	0.61	42±6
S+S	d	1.9-2.3	9	14.2±2.3	2.8±0.6	0.55	50±8
Pb+Pb	t	1.5-1.8	20	0.038±0.004	1/0.128	0.70	59±3
Pb+Pb	t	1.5-1.8	10	0.037±0.006	1/0.114	0.70	60±4
Pb+Pb	$\pi$ -HBT	2.5-3.1	15				76±9
Pb+Pb	$\pi$ -HBT		5				83±21

The two last lines are HBT results from [10,19]

than  $T_p$  (Table 1) and have been ignored in fitting (12). The volume of homogeneity was then found by fitting  $\alpha$  in the expression

$$B_3 = \alpha \frac{1}{M_t^2} \exp((M_t - M)/T_p) \quad (13)$$

to the data (see Fig. 11) with the relation

$$R_{\perp}^2 R_{\parallel} = \left( \frac{0.01901 \langle C_t \rangle}{\alpha} \right)^{\frac{1}{2}}. \quad (14)$$

The values for  $T_p$  were from Table 1 at a field setting of 2 GeV/c, and the quantum mechanical correction factor related to the triton internal structure is  $C_t=0.70$  according to [9]. The  $\alpha$ -values as well as the volumes of homogeneity are quoted in Table 3, where the value for the parameter  $\delta$  is  $1/T_p$  from Table 1 and has not been fitted. The uncertainties quoted on the volumes of homogeneity are those from the fitting procedure only, and do not include any systematic uncertainties. In the triton case the two most important sources of systematic uncertainties, are the feed down corrections and the use of a fixed value for  $T_p$ . The feed down corrections enter in the power  $\frac{3}{2}$  in the derived volume and the derived  $\alpha$  value depends sensitively on  $T_p$ . The uncertainties quoted in Table 1 for  $T_p$  corresponds to a 20% uncertainty on the derived volume. Typical values for the systematic uncertainties are 20% for volumes derived from deuterons and 30% for the triton volumes. It should also be pointed out, that the  $T_p$  values come from fitting the proton spectra at very small  $m_t - m$  values (0.02-0.05 GeV/c<sup>2</sup>) and probably are not characteristic of the spectra as a whole. The triton volumes in the rapidity interval 1.5-1.8 are somewhat larger than the deuteron volumes in the 1.4-1.7 interval. The systematic uncertainty from the feed down corrections is unimportant in this comparison, but the uncertainty from  $T_p$  remains, so the differences are less than two standard deviations. There is no demonstrated need for introducing a second composite route in the triton formation ( $p+n+n \rightarrow d+n \rightarrow t$ ) in order to obtain similar volumes of homogeneity for deuterons and tritons.

## 7 Conclusions

The measurements cover deuteron coalescence for three different collision systems, Pb+Pb, S+Pb and S+S, and triton coalescence for the Pb+Pb system. Both deuteron and triton measurements exhibit a dependence on the cluster transverse mass  $M_t$  that yields  $B_A$ -values which increase with increasing  $M_t$ . The deuteron measurements from Pb+Pb show a rapidity dependence opposite of that expected from the single (spherical) source model without expansion. No systematic dependence of the derived  $B_A$ -values on centrality was found.

The main source of systematic uncertainties stem from corrections to the observed proton spectra for feed down from hyperon decays, and these uncertainties tend to dominate over the statistical uncertainties.

The interpretation of the measured cross sections for protons, deuterons and tritons in terms of interaction volumes were based on theoretical models ([8,9]) that explicitly include the effects of collective expansion.

When the Pb+Pb  $B_2$ -values in the rapidity interval from 1.8-2.3 are interpreted in the framework of Scheibl and Heinz [9] the resulting volumes of homogeneity agree with those from HBT measurements when the pion pair  $m_t$  is close to the nucleon mass. The deuteron Pb+Pb volumes of homogeneity depend markedly on rapidity, a feature that disagrees with the model of [9]. The volumes derived for the S collisions are smaller than the Pb+Pb volumes in the same rapidity interval at the two sigma level, ignoring systematic uncertainties.

The Pb+Pb  $B_3$ -values yield volumes of homogeneity that lie between the corresponding volumes from deuterons in the two rapidity ranges covered. Compared to the deuteron volume in the rapidity interval from 1.4–1.7, that is close to the interval for the triton measurements, the triton volume is larger than the deuteron volume, but the difference does not reach a two sigma significance. Thus the Scheibl and Heinz model does not require any substantial contribution to the triton formation from intermediate deuteron formation in contrast to the conclusion

drawn by Polleri [7] from comparisons to a preliminary version of the present data.

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